ECEN689: Special Topics in Optical Interconnects Circuits and Systems Spring 2022

Lecture 5: Transimpedance Amplifiers (TIAs)



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Announcements

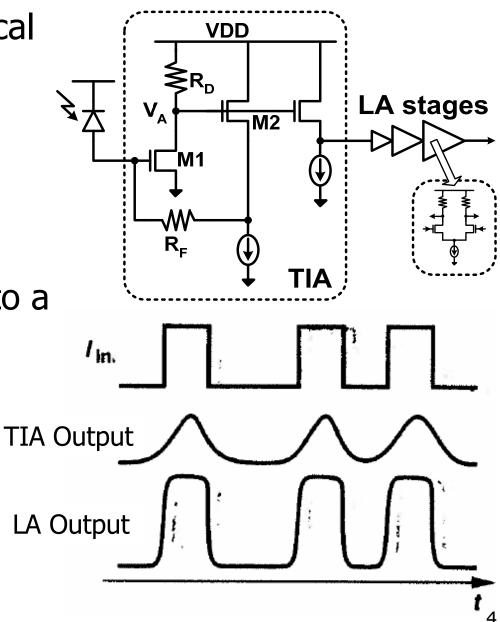
- Homework 2 is posted on website and due today
- Exam 1 Mar 10
 - In class
 - One double-sided 8.5x11 notes page allowed
 - Bring your calculator
 - Covers through Lecture 6
- Reading
 - Sackinger Chapter 5
 - Razavi Chapter 4

Agenda

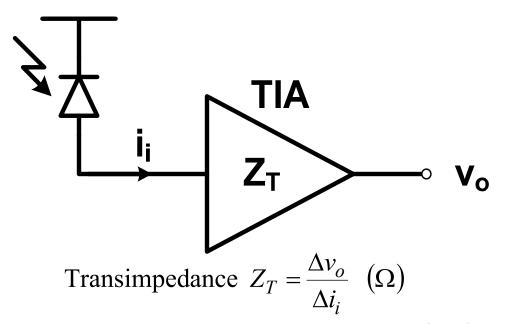
- Optical Receiver Overview
- Transimpedance Amplifiers
 - Common-Gate TIAs
 - Feedback TIAs
 - Common-Gate & Feedback TIA Combinations
 - Differential TIAs
- Integrating Optical Receivers
- Equalization in Optical Front-Ends

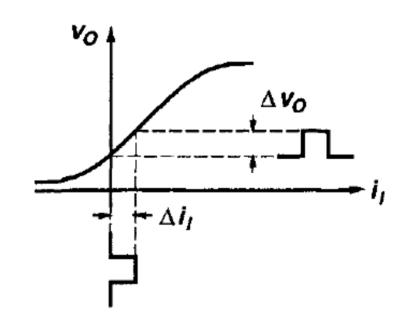
Optical Receiver Technology

- Photodetectors convert optical power into current
 - p-i-n photodiodes
 - Waveguide Ge photodetectors
- Electrical amplifiers then convert the photocurrent into a voltage signal
 - Transimpedance amplifiers
 - Limiting amplifiers
 - Integrating optical receiver



Transimpedance Amplifier (TIA)

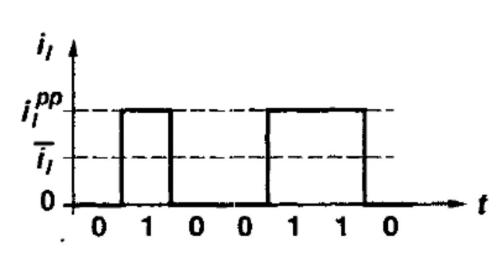


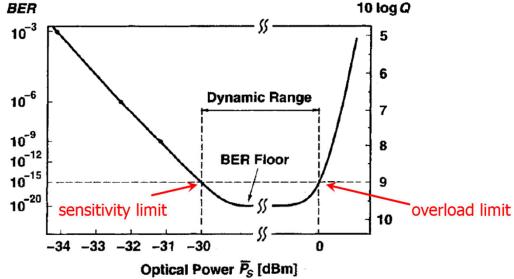


Also expressed in units of dB Ω by $20\log(|Z_T|)$

- Key design objectives
 - High transimpedance gain
 - Low input resistance for high bandwidth and efficient gain
- For large input currents, the TIA gain can compress and pulse-width distortion/jitter can result

Maximum Currents



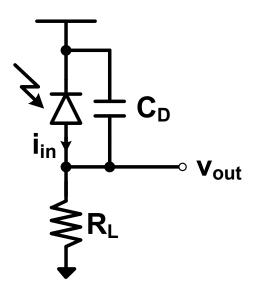


- Input Overload Current
 - The maximum peak-to-peak input current for which we can achieve the desired BER
 - Assuming high extinction ratio $i_{ovl}^{pp} = 2R\overline{P}_{ovl}$
- Maximum Input Current for Linear Operation
 - Often quantified by the current level for a certain gain compression (1dB)

 $i_{lin}^{pp} < i_{ovl}^{pp}$

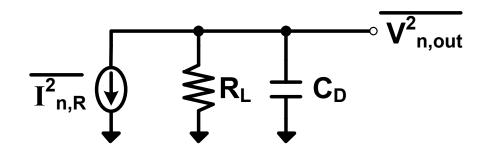
Resistive Front-End

[Razavi]



$$R_T = R_{in} = R_L$$

$$BW_{3dB} = \omega_p = \frac{1}{R_{in}C_D} = \frac{1}{R_LC_D}$$



$$\overline{V_{n,out}^2} = \int_0^\infty \overline{I_n^2} Z_T^2 df = \int_0^\infty \frac{4kT}{R_L} \left(\frac{R}{1+j2\pi fRC}\right)^2 df = \frac{kT}{C_D}$$

$$\overline{I_{n,in}^2} = \frac{\overline{V_{n,out}^2}}{R_L^2} = \frac{kT}{R_L^2 C_D}$$

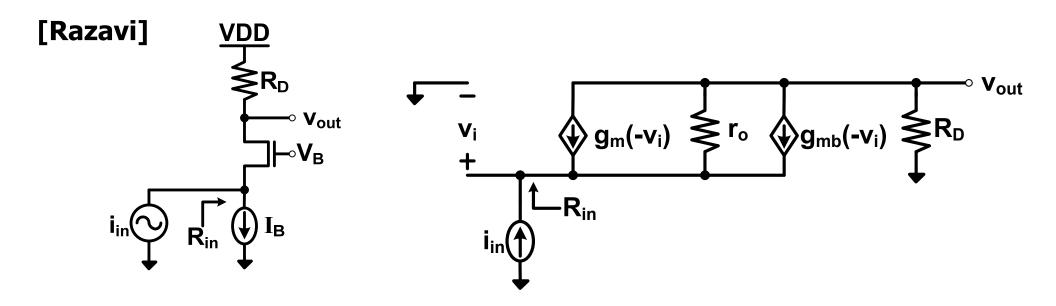
$$I_{n,in,rms} = \frac{\sqrt{KT/C_D}}{R_L}$$

 Direct trade-offs between transimpedance, bandwidth, and noise performance

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Common-Gate TIA

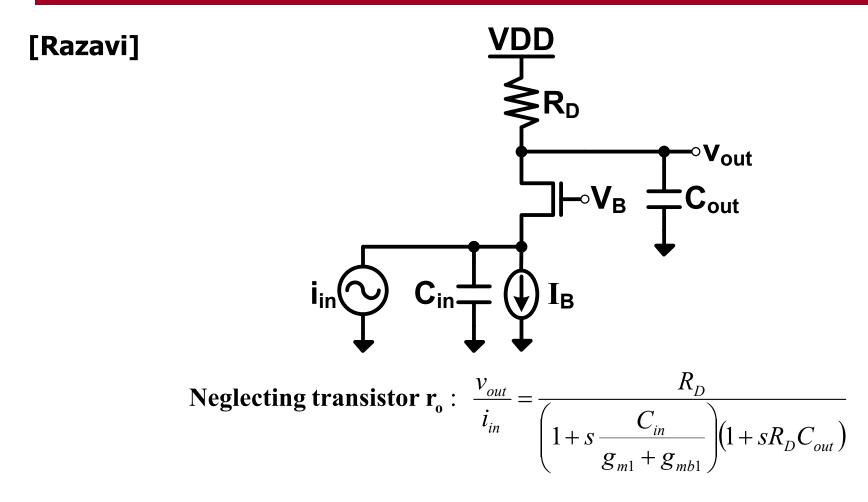


$$R_T = R_D$$

$$R_{in} = \frac{r_o + R_D}{1 + (g_m + g_{mb})r_o} \approx \frac{1}{g_m}$$

 Input resistance (input bandwidth) and transimpedance are decoupled

Common-Gate TIA Frequency Response



 Often the input pole may dominate due to large photodiode capacitance (100 – 500fF)

Common-Gate TIA Noise

[Razavi]

Neglecting transistor r_0 :

$$\overline{V_{n,out}^2} = \left(\overline{I_{n,M2}^2} + \overline{I_{n,RD}^2}\right) R_D^2 = 4kT \left(\frac{2}{3}g_{m2} + \frac{1}{R_D}\right) R_D^2 \quad \left(\frac{\mathbf{V}^2}{\mathbf{Hz}}\right)$$

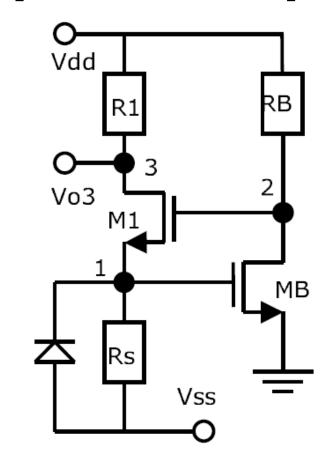
$$\overline{I_{n,in}^2} = 4kT \left(\frac{2}{3}g_{m2} + \frac{1}{R_D}\right) \quad \left(\frac{\mathbf{A}^2}{\mathbf{Hz}}\right)$$

- Both the bias current source and RD contribute to the input noise current
- RD can be increased to reduce noise, but voltage headroom can limit this
- Common-gate TIAs are generally not for low-noise applications
- $\overline{V_{n,out}^2} = \left(\overline{I_{n,M2}^2} + \overline{I_{n,RD}^2}\right)R_D^2 = 4kT\left(\frac{2}{3}g_{m2} + \frac{1}{R_D}\right)R_D^2 \quad \left(\frac{\mathbf{V}^2}{\mathbf{Hz}}\right) \quad \text{However, they are relatively}$ simple to design with high stability

Regulated Cascode (RGC) TIA

- Input transistor gm is boosted by commonsource amplifier gain, resulting in reduced input resistance
- Requires additional voltage headroom
- Increased input-referred noise from the commonsource stage

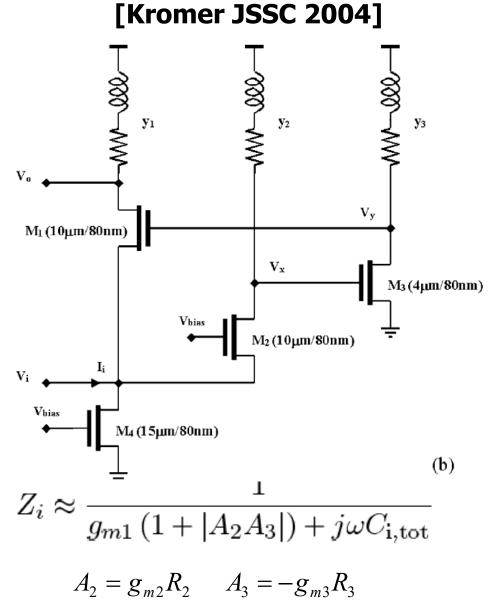
[Park ESSCIRC 2000]



$$Z_{in}(0) \cong \frac{1}{g_{m1}(1+g_{mB}R_B)}$$

CMOS 20GHz TIA

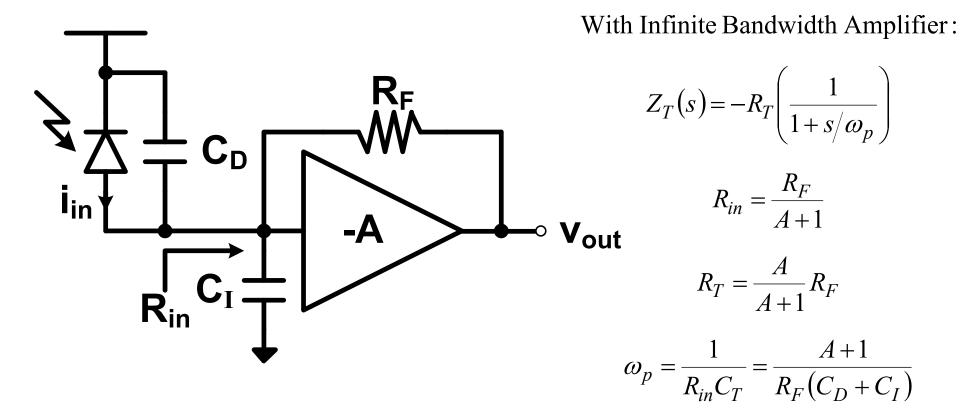
- An additional commongate stage in the feedback provides further gm-boosting and even lower input resistance
- Shunt-peaking inductors provide bandwidth extension at zero power cost, but very large area cost



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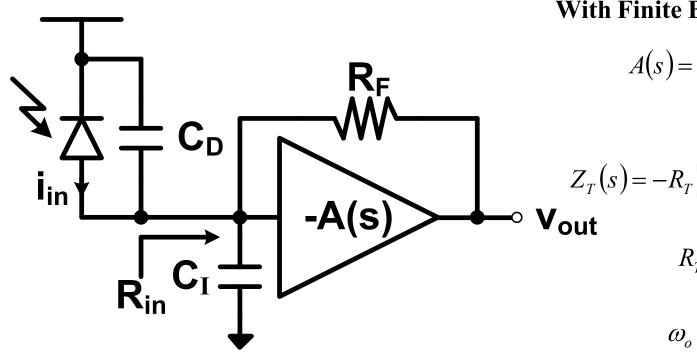
Feedback TIA w/ Ideal Amplifier



- Input bandwidth is extended by the factor A+1
- Transimpedance is approximately R_F
- Can make R_F large without worrying about voltage headroom considerations

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Feedback TIA w/ Finite Bandwidth Amplifier



 Finite bandwidth amplifier modifies the transimpedance transfer function to a secondorder low-pass function

With Finite Bandwidth Amplifier:

$$A(s) = \frac{A}{1 + \frac{s}{\omega_A}} = \frac{A}{1 + sT_A}$$

$$Z_T(s) = -R_T \left(\frac{1}{1 + s/(\omega_o Q) + s^2/\omega_o^2} \right)$$
Vout
$$R_T = \frac{A}{A+1} R_F$$

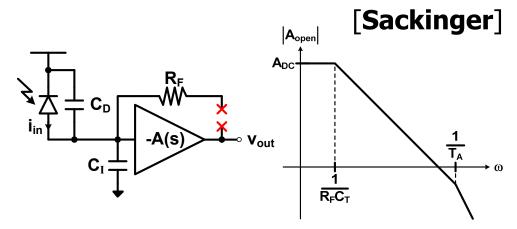
$$\omega_o = \sqrt{\frac{A+1}{R_F C_T T_A}}$$

$$Q = \frac{\sqrt{(A+1)R_F C_T T_A}}{R_F C_T + T_A}$$

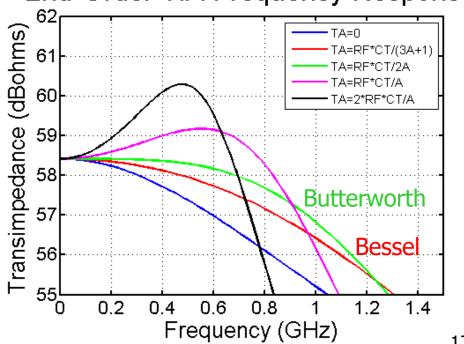
$$R_{in} = \frac{R_F}{A+1}$$

Feedback TIA w/ Finite Bandwidth Amplifier

- Non-zero amplifier time constant can actually increase TIA bandwidth!!
- However, can result in peaking in frequency domain and overshoot/ringing in time domain
- Often either a Butterworth (Q=1/sqrt(2)) or Bessel response (Q=1/sqrt(3)) is used
 - Butterworth gives maximally flat frequency response
 - Bessel gives maximally flat groupdelay



2nd-Order TIA Frequency Response



Feedback TIA Transimpedance Limit

If we assume a Butterworth response for mazimally flat frequency response:

$$Q = \frac{1}{\sqrt{2}} \qquad \Rightarrow \qquad \omega_A = \frac{1}{T_A} = \frac{2A}{R_F C_T}$$

For a Butterworth response:

$$\omega_{3\text{dB}} = \omega_0 = \sqrt{\frac{(A+1)\omega_A}{R_F C_T}} = \frac{\sqrt{(A+1)2A}}{R_F C_T} \approx \sqrt{2} \text{ times larger than } T_A = 0 \text{ case of } \frac{A+1}{R_F C_T}$$

Plugging $R_T = \frac{A}{A+1}R_F$ into above expression yields the maximum possible R_T for a given bandwidth

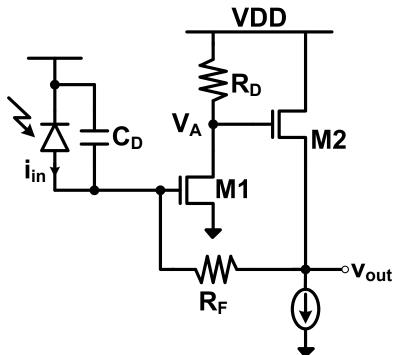
$$\sqrt{\frac{(A+1)\omega_A}{\left(\frac{A+1}{A}\right)}R_TC_T} \ge \omega_{3dB}$$

$$\mathbf{Maximum} \ R_T \le \frac{A\omega_A}{C_T\omega_{3dB}^2}$$

[Mohan JSSC 2000]

- Maximum R_T proportional to amp gain-bandwidth product
- If amp GBW is limited by technology f_T, then in order to increase bandwidth, R_T must decrease quadratically!

Feedback TIA



Assuming that the source follower has an ideal gain of 1

$$A = g_{m1}R_{D}$$

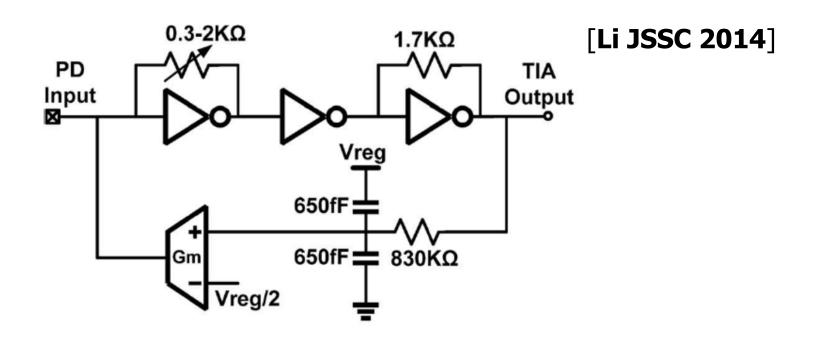
$$R_{T} = \frac{g_{m1}R_{D}}{1 + g_{m1}R_{D}}R_{F}$$

$$R_{in} = \frac{R_{F}}{1 + g_{m1}R_{D}}$$

$$R_{out} = \frac{1}{g_{m2}(1 + g_{m1}R_{D})}$$

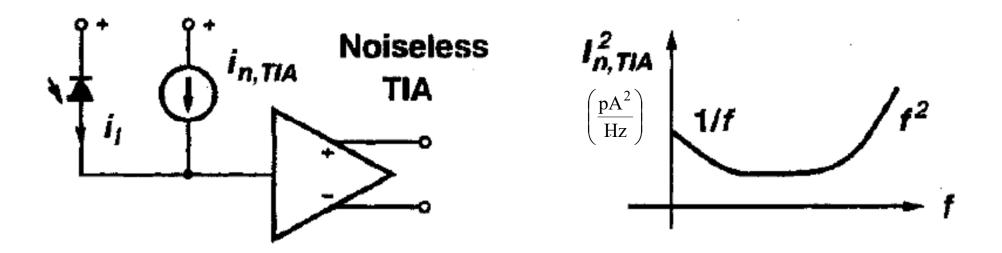
 As power supply voltages drop, there is not much headroom left for RD and the amplifier gain degrades

CMOS Inverter-Based Feedback TIA



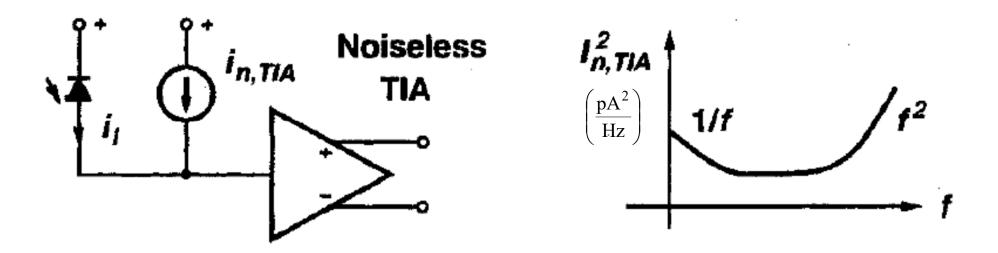
- CMOS inverter-based TIAs allow for reduced voltage headroom operation
- Cascaded inverter-gm + TIA stage provide additional voltage gain
- Low-bandwidth feedback loop sets the amplifier output common-mode level

Input-Referred Noise Current



- TIA noise is modeled with an input-referred noise current source that reproduces the output TIA output noise when passed through an ideal noiseless TIA
- This noise source will depend on the source impedance, which is determined mostly by the photodetector capacitance

Input-Referred Noise Current Spectrum



- Input-referred noise current spectrum typically consists of uniform, high-frequency f², & lowfrequency 1/f components
- To compare TIAs, we need to see this noise graph out to ~2X the TIA bandwidth
 - Recall the noise bandwidth tables

Input-Referred RMS Noise Current

 The input-referred rms noise current can be calculated by dividing the rms output noise voltage by the TIA's midband transimpedance value

$$i_{n,TIA}^{rms} = \frac{1}{R_T} \sqrt{\int_0^{>2BW} |Z_T(f)|^2 I_{n,TIA}^2(f) df}$$

- If we integrate the output noise, the upper bound isn't too critical. Often this is infinity for derivations, or 2X the TIA bandwidth in simulation
- This rms current sets the TIA's electrical sensitivity

$$i_{sens}^{pp} = 2Qi_{n,TIA}^{rms}$$

 To determine the total optical receiver sensitivity, we need to consider the detector noise and responsivity

Averaged Input-Referred Noise Current Density

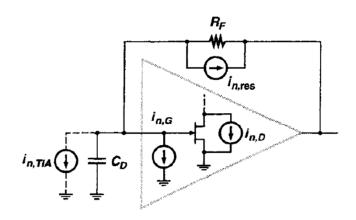
 TIA noise performance can also be quantified by the averaged input-referred noise current density

$$i_{n,TIA}^{avg} = \frac{i_{n,TIA}^{rms}}{\sqrt{BW_{3dB}}}$$

This quantity has units of
$$\left(\frac{pA}{\sqrt{Hz}}\right)$$
.

Note, this is different than averaging the input - referred noise spectrum, $I_{n,TIA}^2(f)$ over the TIA bandwidth.

FET Feedback TIA Input-Referred Noise Current Spectrum



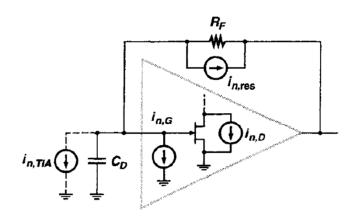
 The feedback resistor and amplifier front-end noise components determine the input-referred noise current spectrum

$$I_{n,TIA}^{2}(f) = I_{n,res}^{2}(f) + I_{n,front}^{2}(f)$$

 The feedback resistor component is uniform with frequency $I_{n,res}^2(f) = \frac{4kT}{R_E}$

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FET Feedback TIA Input-Referred Noise Current Spectrum



Gate current-induced shot noise

$$I_{n,G}^2 = 2qI_G$$

This is typically small for CMOS designs

FET channel noise

$$I_{n,D}^2 = 4kT\Gamma g_m$$

 Γ is the channel noise factor, typically 0.7 - 3 depending on the process.

Input-Referring the FET Channel Noise

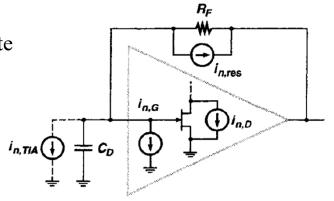
To do this, we could calculate

$$\frac{i_{n,TIA}}{i_{n,D}} = \frac{\left(\frac{v_{out}}{i_{n,D}}\right)}{Z_T}$$

But it is easier (and equivalent) to ground the output and calculate

$$\left(\frac{i_{n,D}}{i_{n,TIA}}\right)^{-1}$$

$$i_{n,D} = g_m v_{n,TIA} = \frac{g_m i_{n,TIA}}{sC_T + \frac{1}{R_F}} = \frac{g_m R_F}{1 + sR_F C_T} i_{n,TIA}$$



where $C_T = C_D + C_I$, the summation of the detector and amplifier input capacitance.

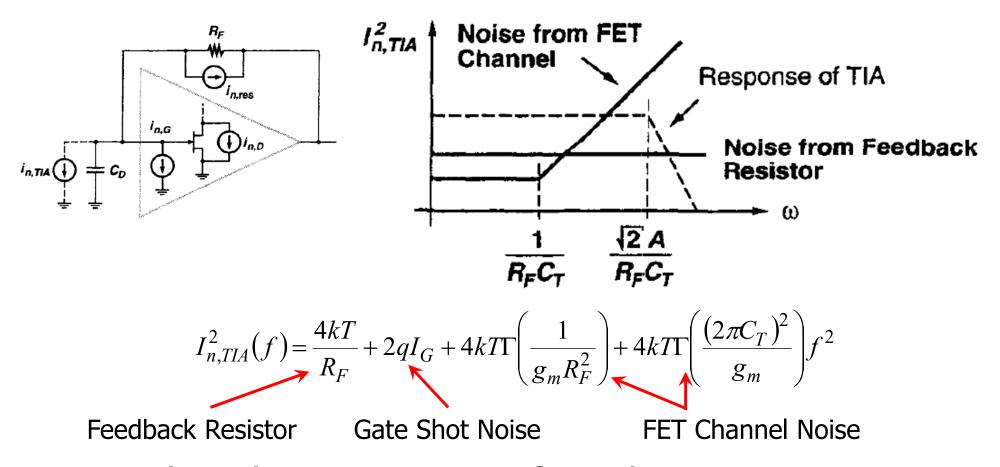
$$\left(\frac{i_{n,D}}{i_{n,TIA}}\right)^{-1} = \frac{1 + sR_FC_T}{g_m R_F}$$

Using this high - pass transfer function, the input - referred FET channel noise is

$$I_{n,front,D}^{2}(f) = \frac{1 + (2\pi f R_{F}C_{T})^{2}}{(g_{m}R_{F})^{2}} \cdot 4kT\Gamma g_{m}$$

$$= 4kT\Gamma \left(\frac{1}{g_{m}R_{F}^{2}}\right) + 4kT\Gamma \left(\frac{(2\pi C_{T})^{2}}{g_{m}}\right) f^{2}$$
Uniform and f² component!

Total Input-Referred FET Feedback TIA Noise

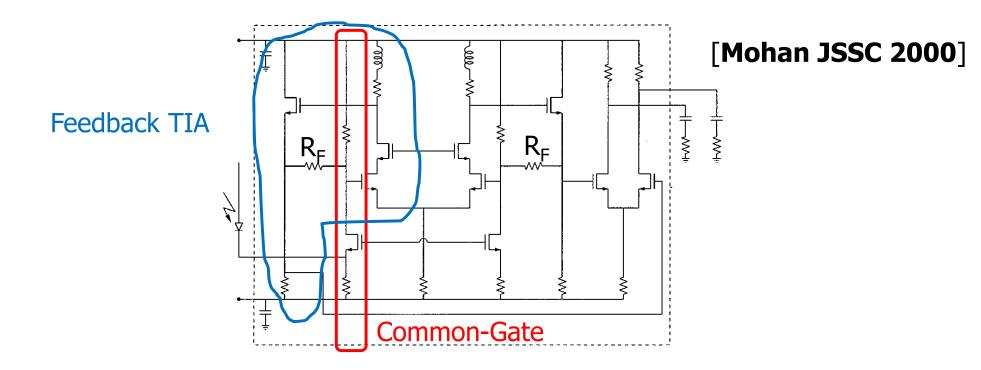


 Note that the TIA input-referred noise current spectrum begins to rise at a frequency lower than the TIA bandwidth

Agenda

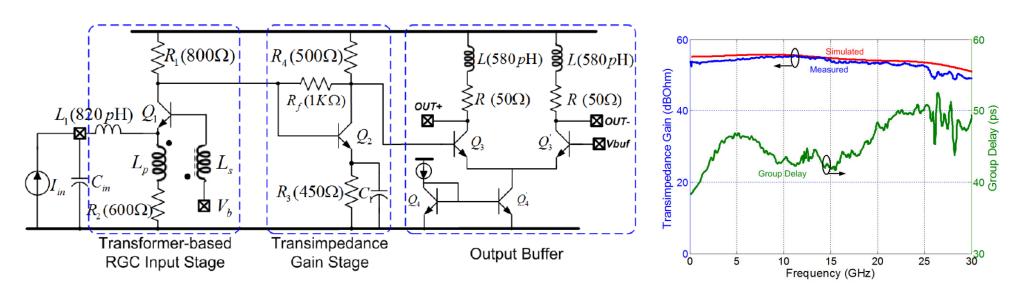
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Common-Gate & Feedback TIA



- Recall that the feedback TIA stability depends on the ratio of the input pole (set by C_D) and the amplifier pole
 - Large variation in C_D can degrade amplifier stability
- Common-gate input stage isolates C_D from input amplifier capacitance, allowing for a stable response with a variety of different photodetectors
- Transimpedance is still approximately R_FA/(1+A)

BJT Common-Base & Feedback TIA



- Transformer-based negative feedback boosts gm with low power and noise overhead
- Input series peaking inductor isolates the photodetector capacitance from the TIA input capacitance
- High frequency techniques allow for 26GHz bandwidth with group delay variation less than 19ps

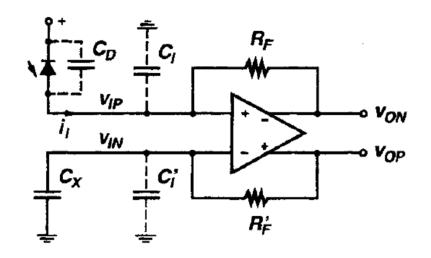
[Li JSSC 2013]

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Differential TIAs

- Differential circuits have superior immunity to power supply/substrate noise
- A differential TIA output allows easy use of common differential main/limiting amplifiers
 - This comes at the cost of higher noise and power
- How to get a differential output with a single-ended photocurrent input?
 - Two common approaches, based on the amount of capacitance applied at the negative input

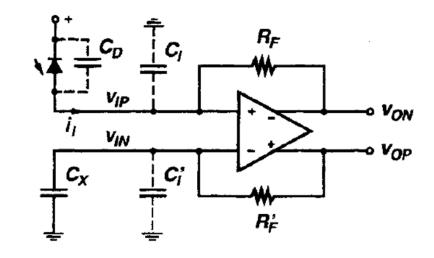


Balanced TIA

 A balanced TIA design attempts to match the capacitance of the two differential inputs

$$C_X \approx C_D$$

- This provides the best power supply/substrate noise immunity, as the noise transfer functions are similar
- Due to double the circuitry, the input-referred rms noise current is increased by sqrt(2)



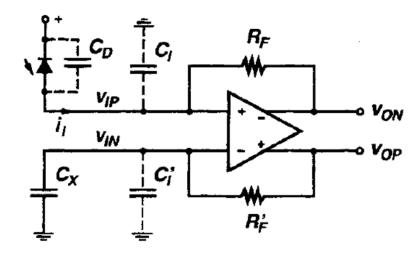
Assuming an high BW amplifier and $C_T = C_D + C_I$

$$Z_T(s) = \frac{v_{OP} - v_{ON}}{i_i} = \frac{\left(\frac{A}{A+1}\right)R_F}{1 + \frac{sC_TR_F}{A+1}}$$

Same transfer function as the single - ended design

Pseudo-Differential TIA

- A pseudo-differential TIA design uses a very large capacitor at the negative input, such that it can be approximated as an AC ground $C_X \to \infty$
- While not good to reject power supply/substrate noise, it does provide significant filtering of the R_F' noise
- The differential transimpedance is approximately doubled relative to the single-ended case



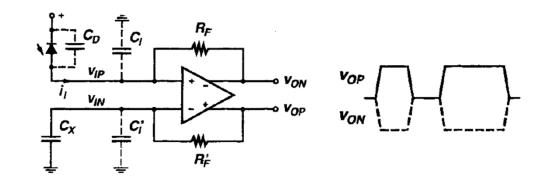
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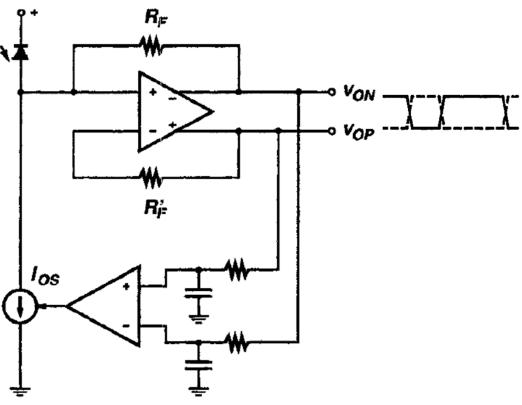
$$Z_{T}(s) = \frac{v_{OP} - v_{ON}}{i_{i}} = \frac{\left(\frac{2A}{A+2}\right)R_{F}}{1 + \frac{sC_{T}R_{F}}{\frac{A}{2}+1}}$$

Offset Control

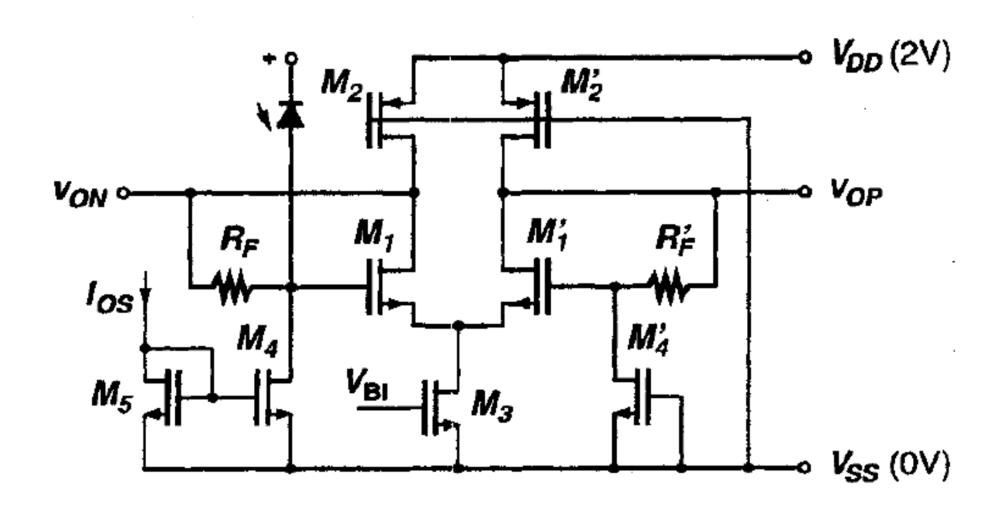
 Due to the single-ended photodetector signal, the differential output signal swings from 0 to V_{ppd}, which can limit the dynamic range

 Adding offset control circuitry can allow for an output swing of ±V_{ppd}/2





Differential Shunt Feedback TIA



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Optical RX Scaling Issues

 Traditionally, TIA has high R_T and low R_{in}

$$R_T = R_F \left(\frac{A}{1+A} \right)$$

$$\omega_{3dB} \approx \frac{1+A}{R_F C_{IN}}$$

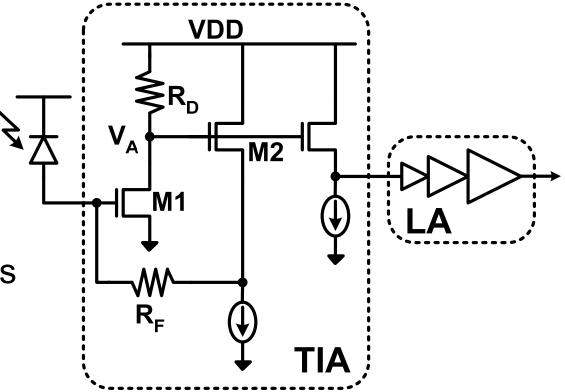
Headrooom/Gain issues in 1V CMOS

•
$$A \approx 2 - 3$$

Power/Area Costs

TIA
$$I_D \propto (R_T C_{IN})^2 f_{3dB}^4$$

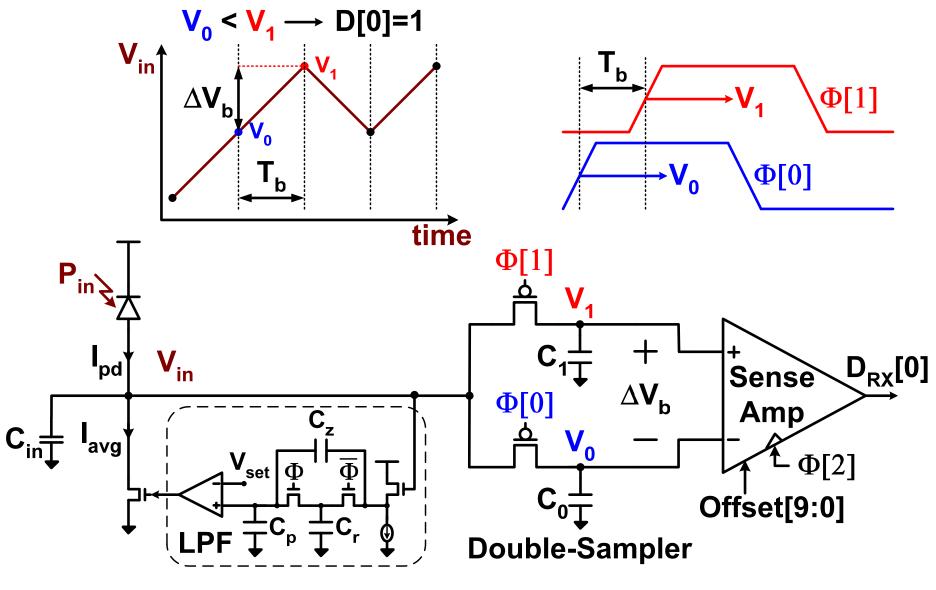
LA
$$I_D \propto f_{3dB}^2$$



$$V_A = V_{GS1} + V_{GS2} \approx 0.8 * VDD$$

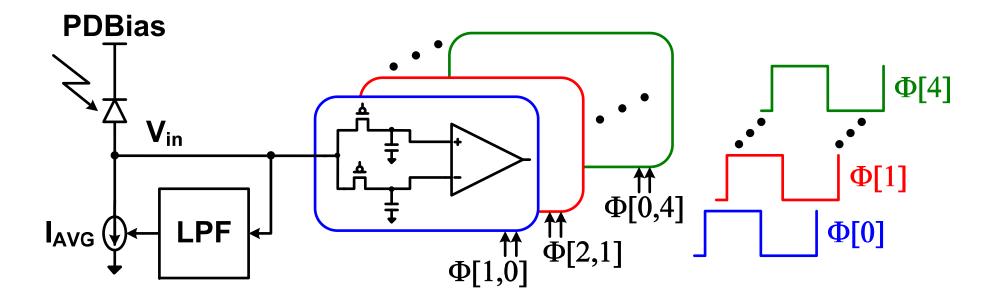
$$A \approx g_{m1}R_D = \frac{\alpha(VDD - V_A)}{VOD} \approx \frac{\alpha(0.2 * VDD)}{VOD}$$

Integrating Receiver Block Diagram



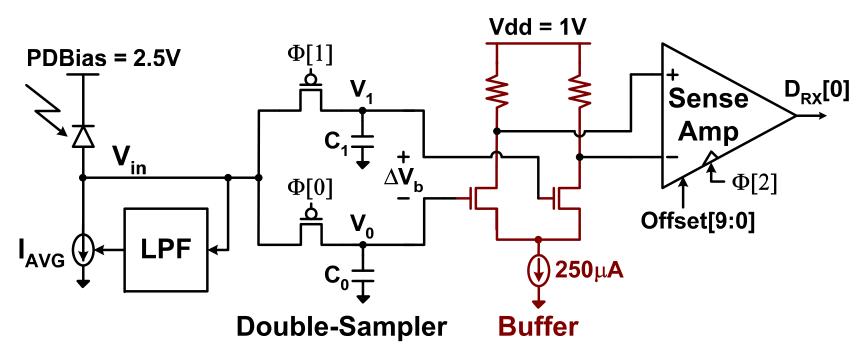
[Emami VLSI 2002]

Demultiplexing Receiver



- Demultiplexing with multiple clock phases allows higher data rate
 - Data Rate = #Clock Phases x Clock Frequency
 - Gives sense-amp time to resolve data
 - Allows continuous data resolution

1V Modified Integrating Receiver

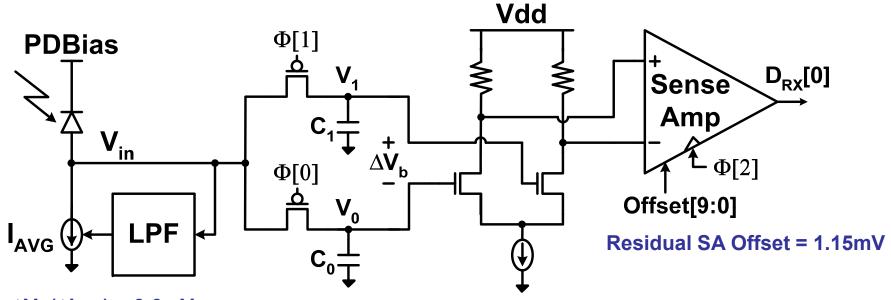


Differential Buffer

- Fixes sense-amp common-mode input for improved speed and offset performance
- Reduces kickback charge
- Cost of extra power and noise

Input Range = 0.6 - 1.1V

Receiver Sensitivity Analysis



 $\sigma_{samp} = \sqrt{\frac{2kT}{C_{samp}}} = 0.92mV \qquad \sigma_{buffer} = 1.03mV \qquad \sigma_{SA} = 0.45mV$

Clock Jitter Noise $\sigma_{clk} = \left(\frac{\sigma_j}{T_b}\right) \Delta v_b \approx 0.65 mV$ at 16Gb/s

Total Input Noise $\sigma_{tot} = \sqrt{\sigma_{samp}^2 + \sigma_{buffer}^2 + \sigma_{SA}^2 + \sigma_{clk}^2} = 1.59 mV$

 ΔV_{b} for BER = 10⁻¹⁰ = 6.4 σ_{tot} + Offset = 11.9mV

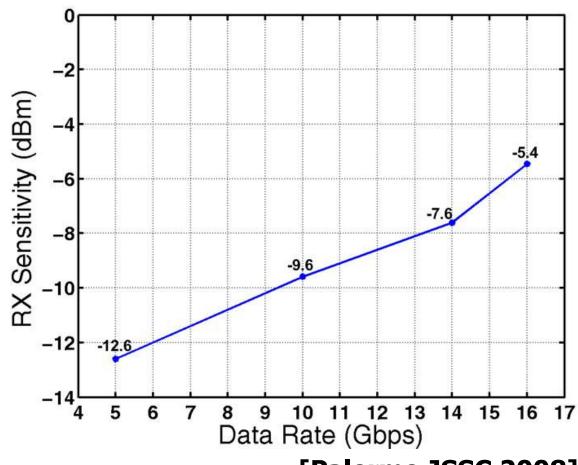
$$P_{avg} = \frac{\Delta V_b \left(C_{pd} + C_{in} \right)}{\rho T_b}$$

Gb/s	P _{avg} (dBm)
10	-9.8
16	-7.8

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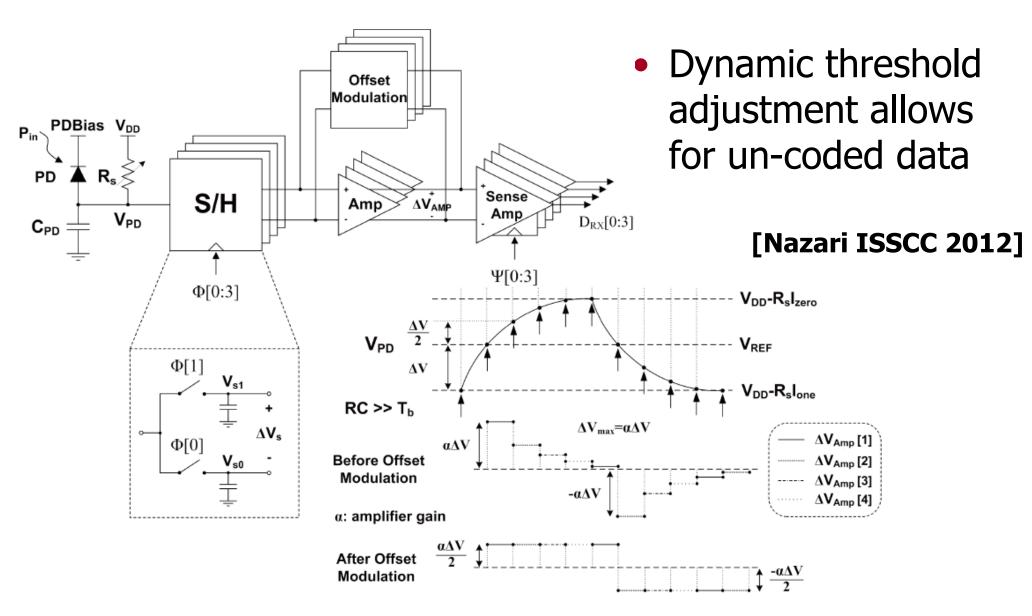
Integrating Receiver Sensitivity

- Test Conditions
 - 8B/10B data patterns (variance of 6 bits)
 - Long runlength data (variance of 10 bits)
- BER $< 10^{-10}$

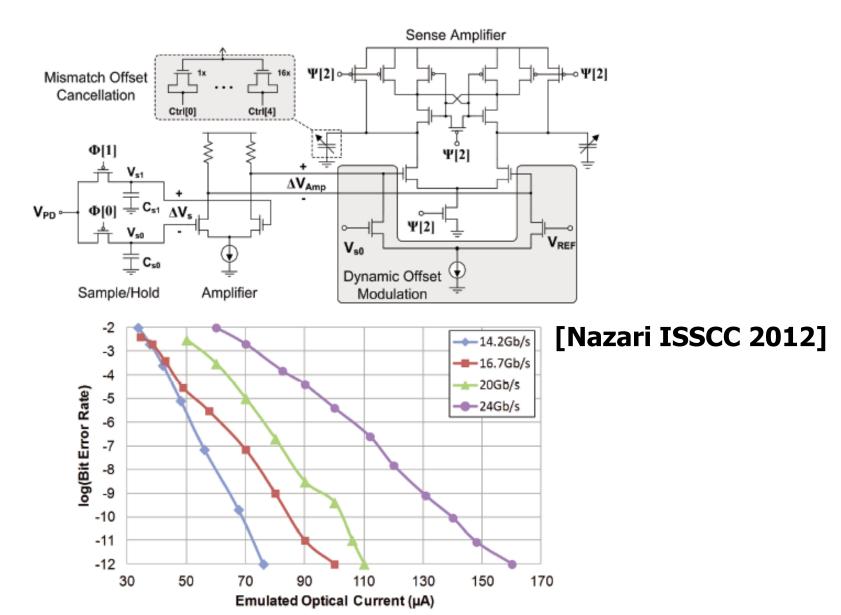


[Palermo JSSC 2008]

Integrating RX with Dynamic Threshold



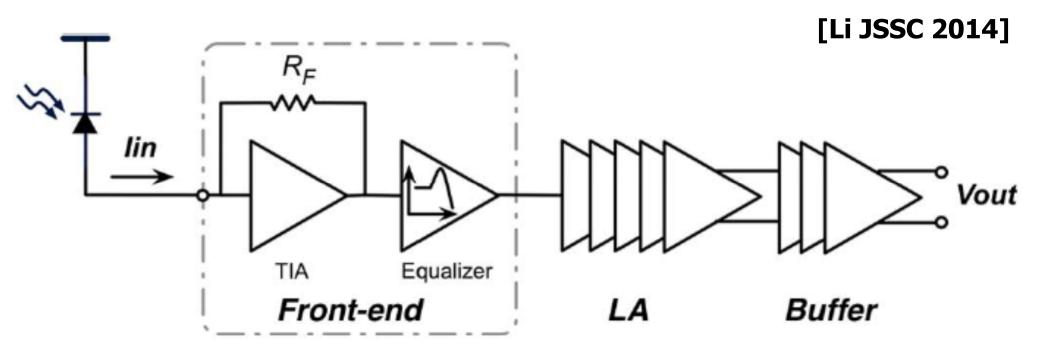
Integrating RX with Dynamic Threshold



Agenda

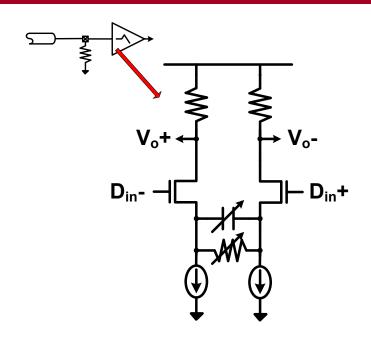
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 - Feedback TIAs
 - Common-Gate & Feedback TIA Combinations
 - Differential TIAs
- Integrating Optical Receivers
- Equalization in Optical Front-Ends

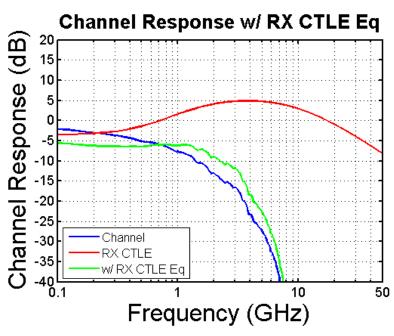
Low-BW TIA & CTLE Front-End

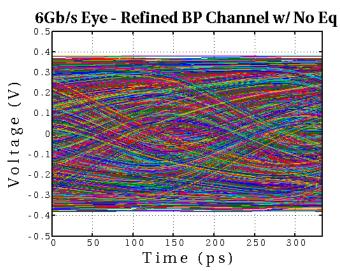


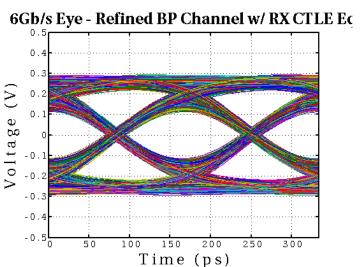
- Improved sensitivity is possible by increasing the first stage feedback resistor, resulting in a high-gain low-bandwidth TIA
- The resultant ISI is cancelled by a subsequent CTLE

Active CTLE Example

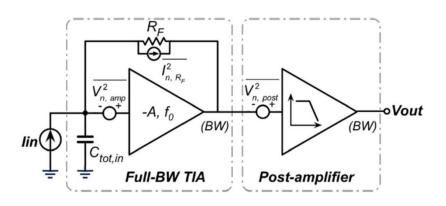


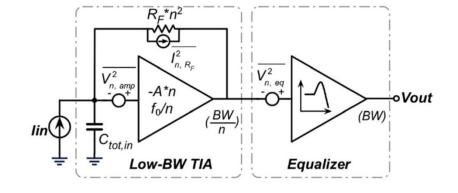




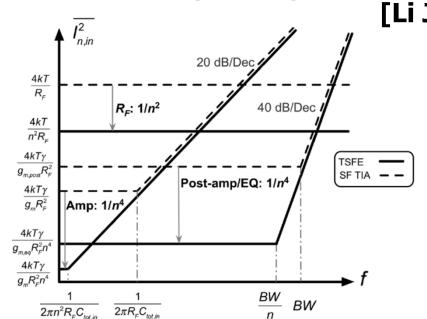


Low-BW TIA & CTLE Front-End



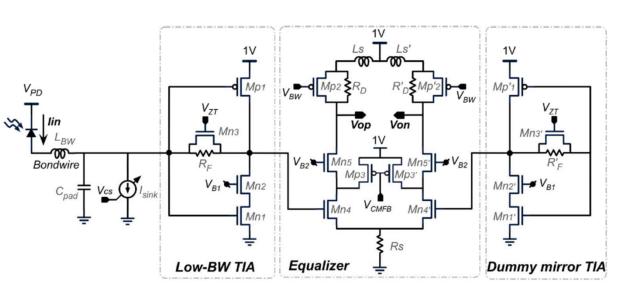


$$\overline{I_{n,\text{in,SF}}^2(f)} = \frac{4kT}{R_F} + \frac{4kT\gamma}{g_m R_F^2} + 4kT\gamma \frac{(2\pi C_{\text{tot,in}})^2}{g_m} f^2 + \frac{4kT\gamma}{g_{m,\text{post}} R_F^2} + \frac{4kT\gamma}{g_{m,\text{post}} R_F^2} \left(\frac{f}{BW}\right)^4$$

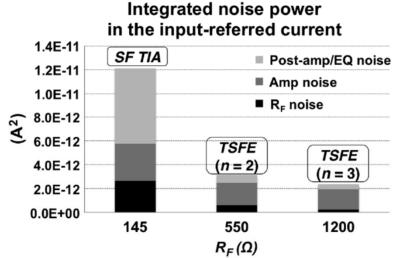


- $\overline{I_{n,\text{in,TSFE}}^2(f)} = \frac{4kT}{R_F n^2} + \frac{4kT\gamma}{a_m R_T^2 n^4}$ $+4kT\gamma \frac{\left(2\pi R_F n^2 C_{\text{tot,in}}\right)^2}{g_m R_F^2 n^4} f^2$ [Li JSSC 2014] $+ \frac{4kT\gamma}{a_{m,eq}R_F^2n^4} + \frac{4kT\gamma}{g_{m,eq}R_F^2n^4} \left(\frac{f}{BW/n}\right)^*$ $= \frac{4kT}{R_{\rm F}n^2} + \frac{4kT\gamma}{aR_{\rm -}^2n^4} + 4kT\gamma \frac{(2\pi C_{\rm tot,in})^2}{a_{\rm res}} f^2$ $+\frac{4kT\gamma}{a_{m,co}R_{p}^{2}n^{4}} + \frac{4kT\gamma}{a_{m,co}R_{p}^{2}} \left(\frac{f}{BW}\right)^{4} \tag{5}$
 - Significant reduction in feedback resistor noise
 - Low-frequency input and post amplifier noise is also reduced

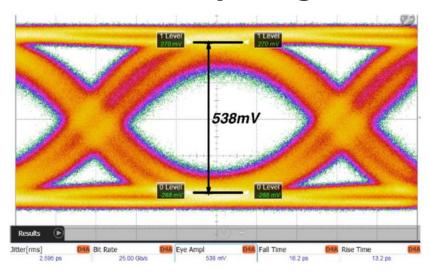
Low-BW TIA & CTLE Front-End

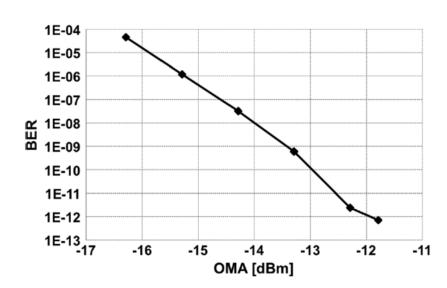


[Li JSSC 2014]



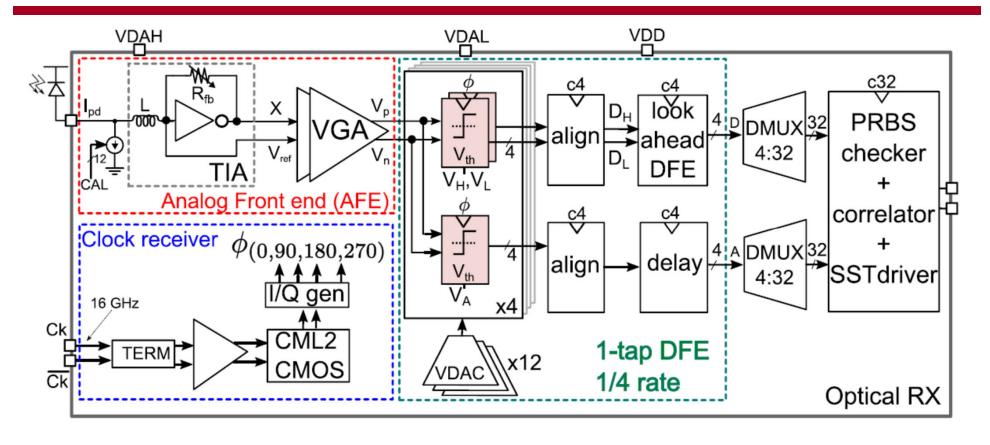
25Gb/s Eye Diagram





Low-BW TIA & DFE RX

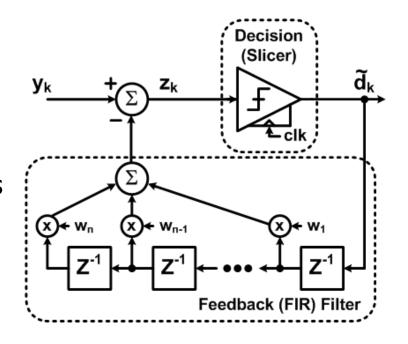
[Ozkaya JSSC 2017]

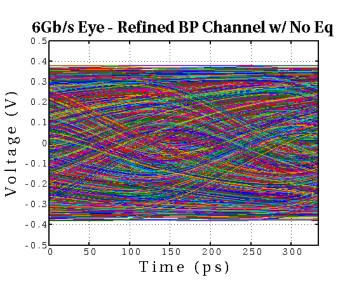


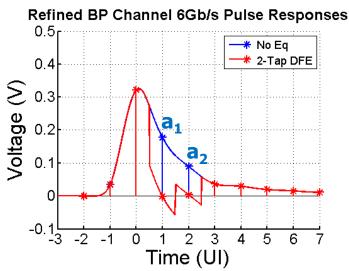
- In a similar manner, a high-gain low-bandwidth TIA is utilized
- The resultant ISI is cancelled by a subsequent 1-tap loopunrolled DFE

DFE Example

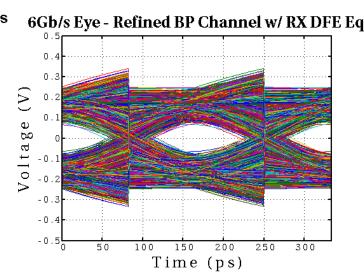
- If only DFE equalization, DFE tap coefficients should equal the unequalized channel pulse response values $[a_1 \ a_2 \ ... \ a_n]$
- With other equalization, DFE tap coefficients should equal the pre-DFE pulse response values
 - DFE provides flexibility in the optimization of other equalizer circuits
 - i.e., you can optimize a TX equalizer without caring about the ISI terms that the DFE will take care of



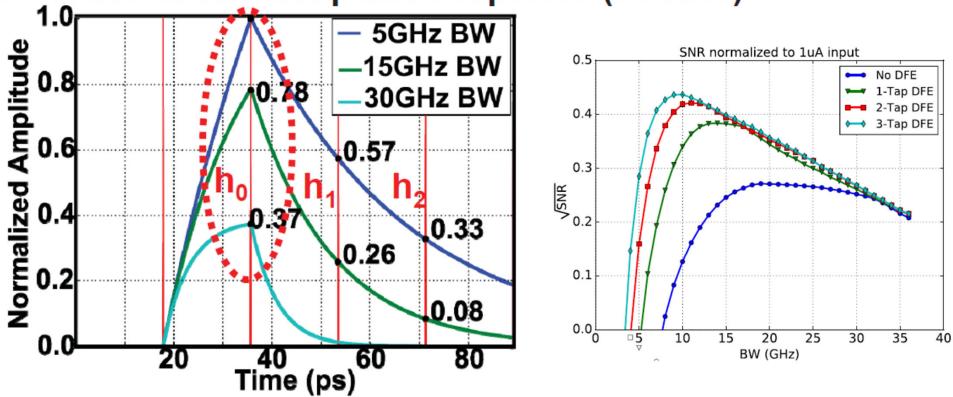




 $[w_1 \ w_2] = [a_1 \ a_2]$



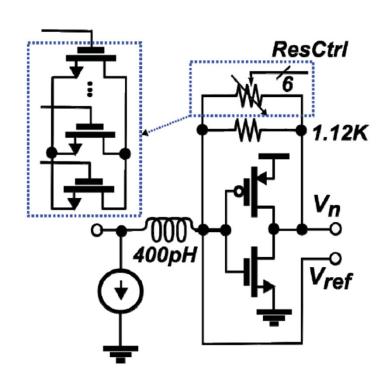
1st order TIA model pulse response (56Gb/s)



- As RF is increased, the main cursor increases and the SNR improves is ISI is cancelled by a DFE
- Large performance benefit with a low-complexity 1-tap DFE

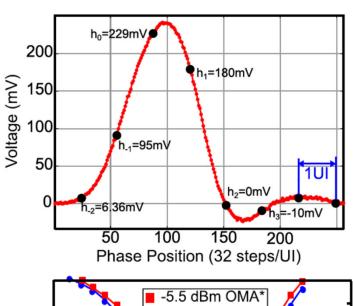
Low-BW TIA & DFE RX

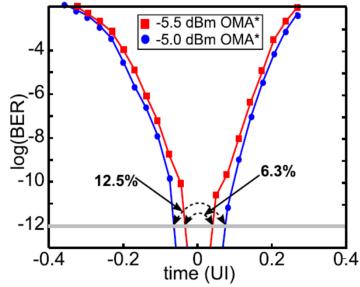
[Ozkaya JSSC 2017]



- Self-referenced TIA is used for differential generation
- Actual 64Gb/s pulse response has a significant pre-cursor ISI tap, which requires a 2-tap TX FFE

64Gb/s Pulse Response & Timing Margin





Next Time

Main/Limiting Amplifiers