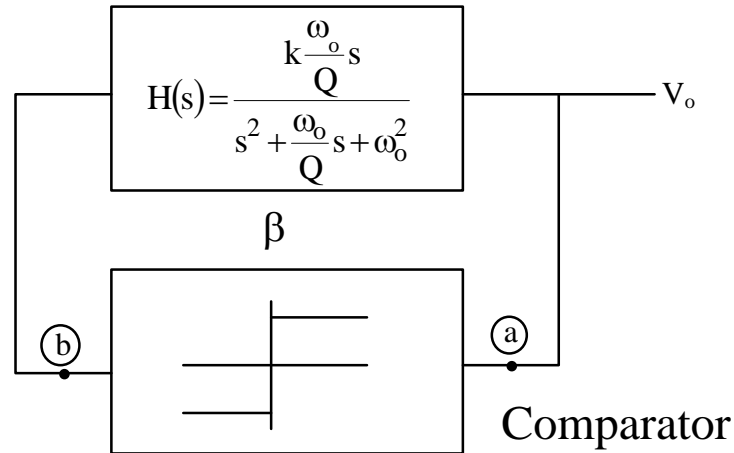


SIGNAL GENERATORS

- SINUSOIDAL
 - BP (Two integrator) Based
 - One Op Amp (Wien-Bridge)
- EXPONENTIAL, TRIANGULAR AND SQUARE WAVE

How to make a sinusoidal oscillator based on filters?

Band Pass Based Oscillator



Assuming small signal conditions, we can write the loop filter

$$1 - \beta H(s) = 0 \quad ; \quad K = k \frac{\omega_o}{Q}$$

$$1 - \frac{sK'}{s^2 + \frac{\omega_o}{Q} s + \omega_o^2} = 0 \quad \text{or} \quad \beta H(s) = 1$$

Thus the characteristic equation-yields:

$$s^2 - \left(K' - \frac{\omega_o}{Q} \right) s + \omega_o^2 = 0$$

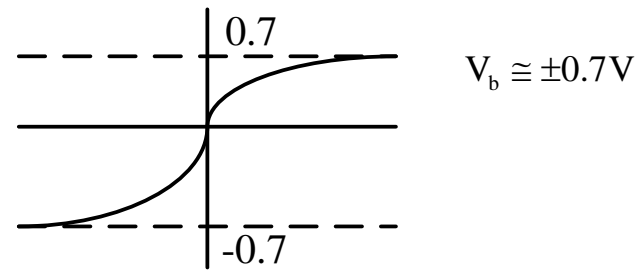
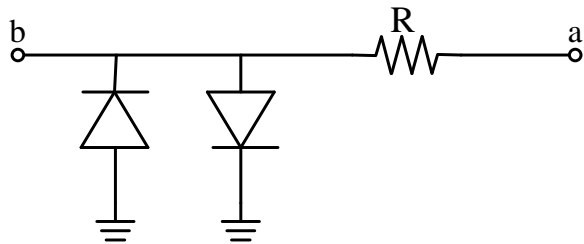
In order to have the poles in the RHP, it is imposed that

$$K' - \frac{\omega_o}{Q} > 0 \quad \text{or} \quad K' \geq \frac{\omega_o}{Q}$$

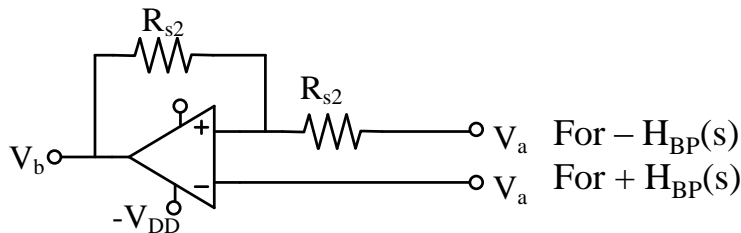
where $K' = K_C K$ and $K_C = V_{\text{sat}} / \Delta V_{\text{TH}}$

However to move the poles on the $j\omega$ axis we require a non-linear block implementation of β . There are a number of blocks to accomplish this.

Implementation 1



Implementation 2

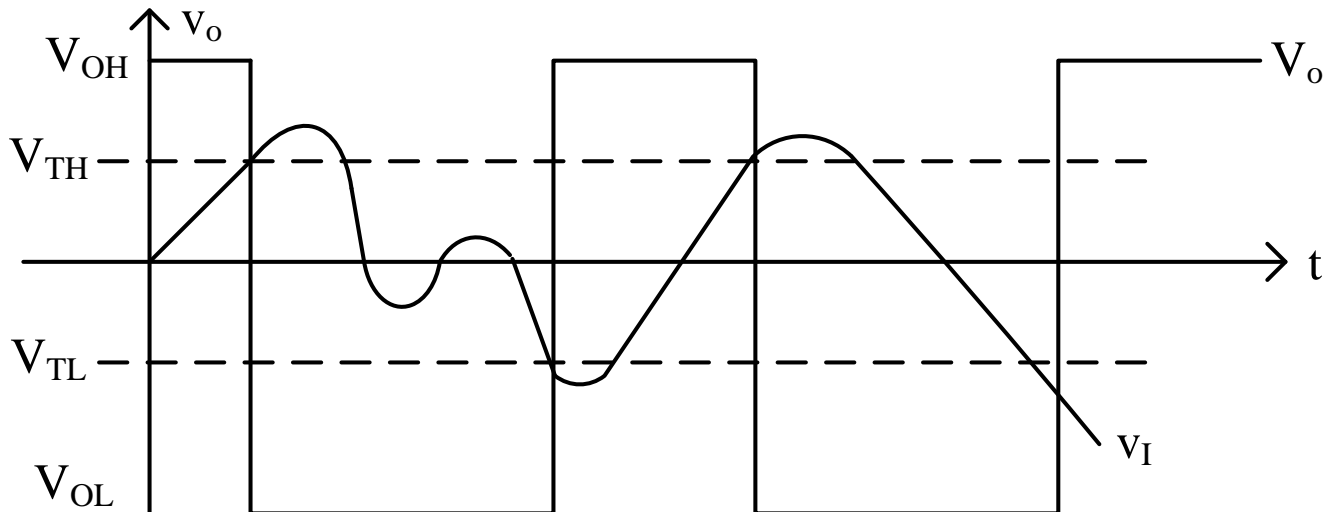
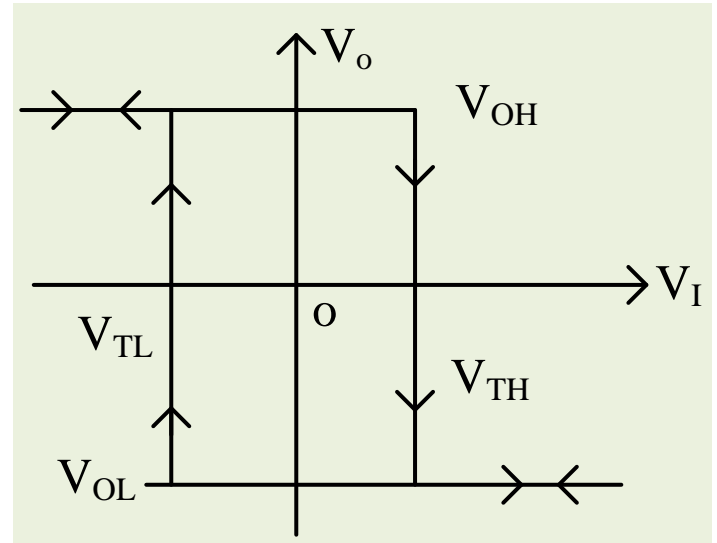
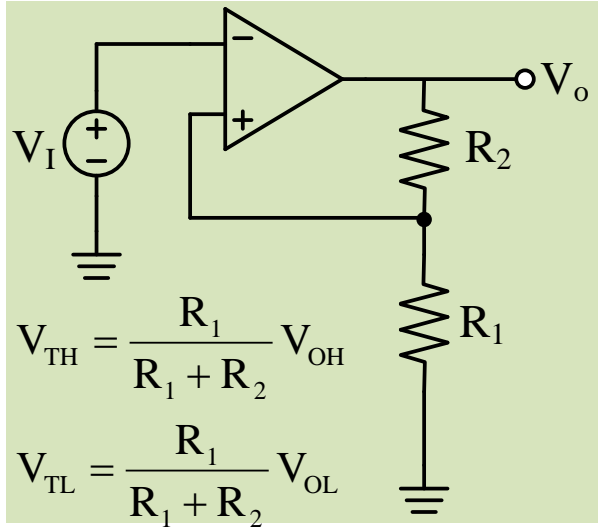


$$K_C = \frac{V_{\text{DD}}}{\Delta V_{\text{TH}}} \cong \frac{V_{\text{DD}}}{\frac{R_1}{R_2} (V_{\text{DD}} - (-V_{\text{DD}}))}$$

$$K_C \cong \frac{R_{s2}}{2R_{s1}}$$

Inverting Schmitt Trigger

Inverting Schmitt Trigger



$$V_{TH} = \frac{R_1}{R_1 + R_2} V_{OH} \quad \text{or} \quad V_{OH} = \left(1 + \frac{R_2}{R_1}\right) V_{TH}$$

$$V_{TL} = \frac{R_1}{R_1 + R_2} V_{OL} \quad \text{or} \quad V_{OL} = \left(1 + \frac{R_2}{R_1}\right) V_{TL}$$

Hysteresis (window) Width:

$$\Delta V_T = V_{TH} - V_{TL} = \frac{R_1}{R_1 + R_2} (V_{OH} - V_{OL})$$

or

$$V_{OH} - V_{OL} = \left(1 + \frac{R_2}{R_1}\right) \Delta V_T$$

Numerical Example

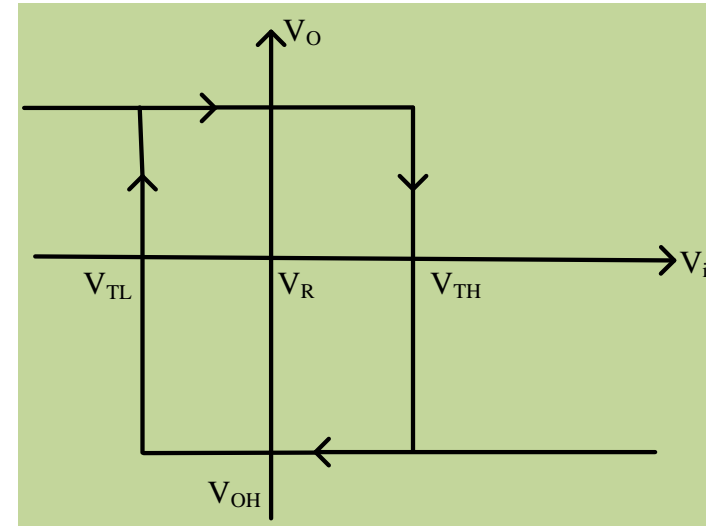
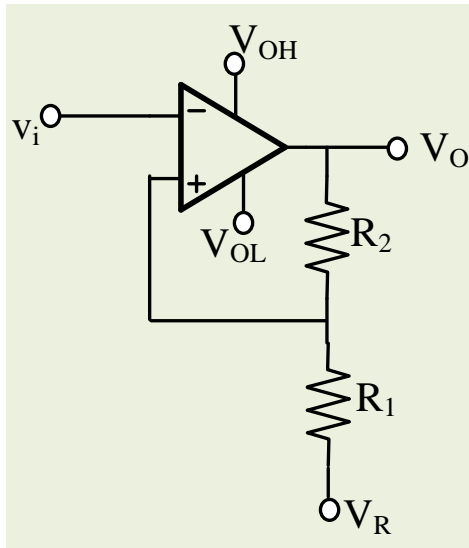
$$V_{OH} = 13V \quad ; \quad V_{OL} = -13V$$

for $R_2 = 16K\Omega$ and $R_1 = 10K\Omega$

$$V_{TH} = \frac{13}{26} \times 10 = 5V$$

$$V_{TL} = \frac{-13}{26} \times 10 = -5V$$

INVERTING SCHMITT TRIGGER WITH REFERENCE VOLTAGE



$$V_{TH} = \frac{V_{OH}R_1 + V_R R_2}{R_1 + R_2} = \frac{V_R + \frac{R_1}{R_2} V_{OH}}{1 + \frac{R_1}{R_2}}$$

$$V_{TL} = \frac{V_{OL}R_1 + V_R R_2}{R_1 + R_2} = \frac{V_R + \frac{R_1}{R_2} V_{OL}}{1 + \frac{R_1}{R_2}}$$

$$\Delta V_T = \frac{\frac{R_1}{R_2}}{1 + \frac{R_1}{R_2}} (V_{OH} - V_{OL}) = \frac{R_1}{R_1 + R_2} (V_{OH} - V_{OL})$$

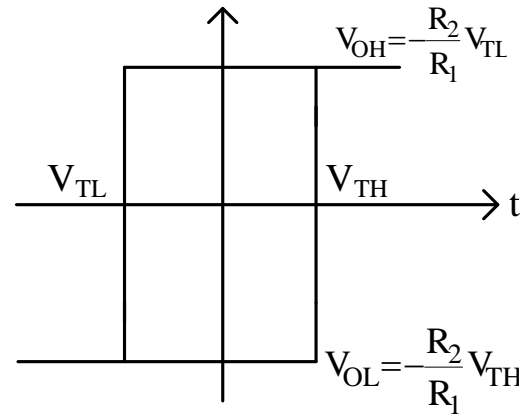
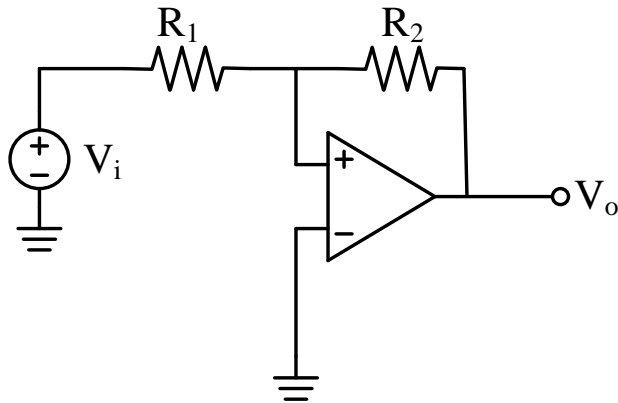
Reader. Exchange input and reference terminals in the figure of Previous page and prove that for the non-inverting comparator

$$V_{TH} = \frac{R_1}{R_2} V_{OH} + V_R \left(1 + \frac{R_1}{R_2} \right)$$

$$V_{LH} = \frac{R_1}{R_2} V_{OL} + V_R \left(1 + \frac{R_1}{R_2} \right)$$

$$\Delta V_T = \frac{R_1}{R_2} (V_{OH} - V_{OL})$$

Non-Inverting Schmitt Trigger

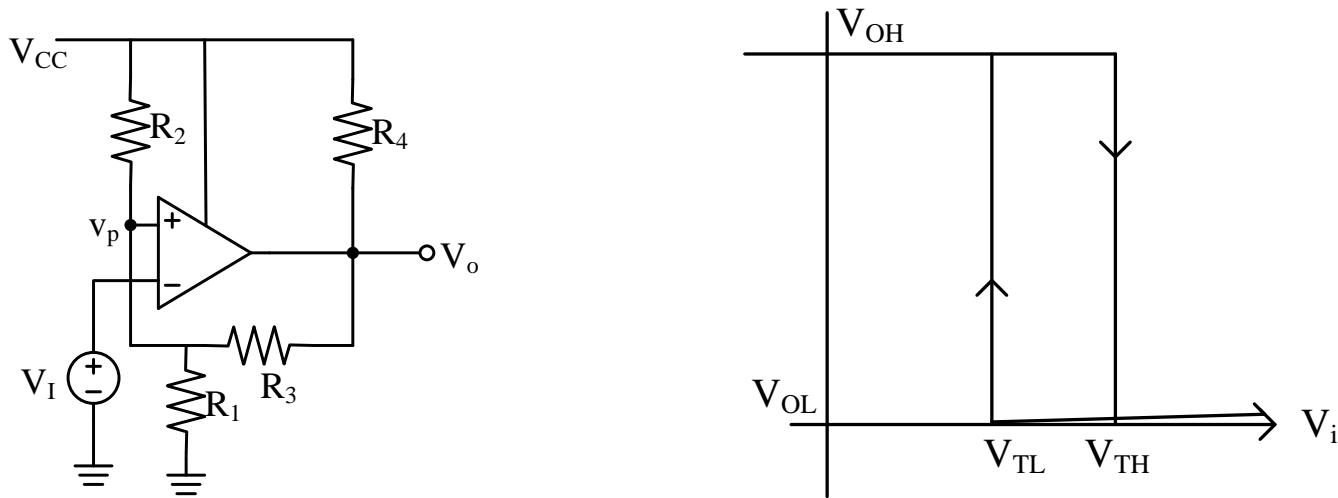


$$V_{TH} = -\frac{R_1}{R_2} V_{OL} \Leftarrow \frac{V_{TH} - 0}{R_1} = \frac{0 - V_{OL}}{R_2}$$

$$V_{TL} = -\frac{R_1}{R_2} V_{OH}$$

$$\Delta V_T = \frac{R_1}{R_2} (V_{OH} - V_{OL}) \quad \text{Hysteresis Window}$$

Schmitt Trigger in I/O in first quadrant and having a single supply.



Using Superposition

$$V_p = \frac{R_{1,3}}{R_{1,3} + R_2} V_{CC} + \frac{R_{1,2}}{R_{1,2} + R_3} V_o$$

where $R_{1,3} = R_1 // R_3$ and $R_{1,2} = R_1 // R_2$

If $V_{OH} \cong V_{CC}$ and $V_{OL} = 0$

then $R_4 \ll R_3 + R_{1,2}$

thus, imposing $V_p = V_{TL}$ for $V_o = V_{OL} = 0$

and $v_p = V_{TH}$ for $V_o = V_{OH} = V_{CC}$, we get

$$V_{TL} = \frac{R_{1,3}}{R_{1,3} + R_2} V_{CC} ; V_{TH} = \frac{R_1}{R_1 + R_{2,3}} V_{CC}$$

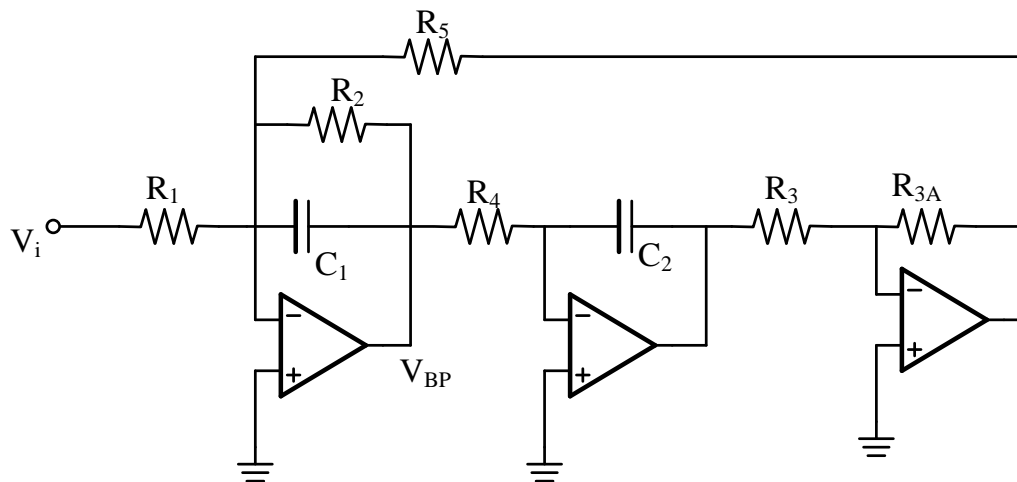
Rearranging terms and fix R_4 and $R_3 \ll R_4$

$$\frac{1}{R_2} = \frac{V_{TL}}{V_{CC} - V_{TL}} \left(\frac{1}{R_1} + \frac{1}{R_3} \right)$$

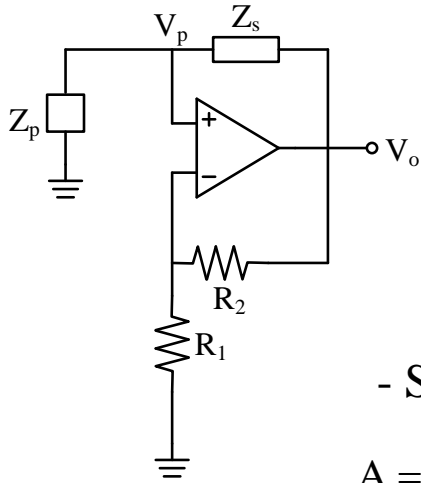
$$\frac{1}{R_1} = \frac{V_{CC} - V_{TH}}{V_{TH}} \left(\frac{1}{R_2} + \frac{1}{R_3} \right)$$

Thus the two above equations can be solved.

The BP in page1 can be implemented using the Tow-Thomas

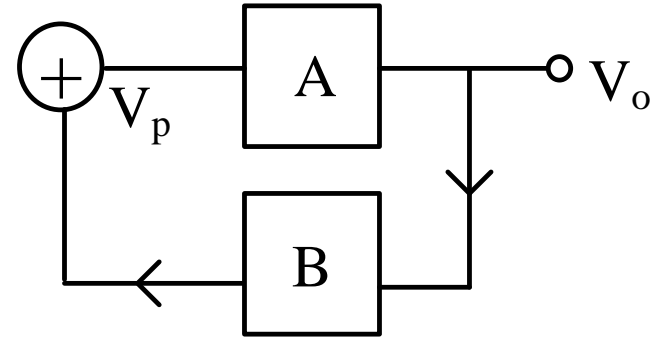


WIEN-BRIDGE OSCILLATOR

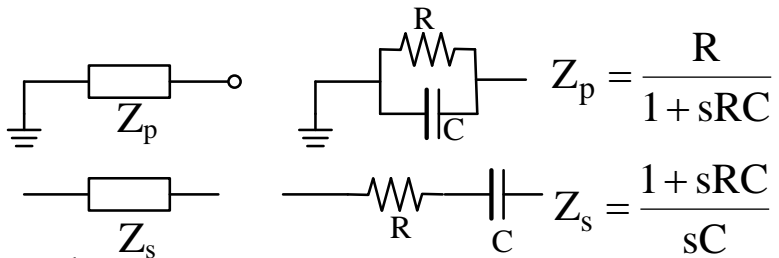


- Seen as non-inverter

$$A = \frac{V_o}{V_p} = 1 + \frac{R_2}{R_1}$$



Furthermore we can see V_p a voltage divider $\frac{Z_p}{Z_p + Z_s} V_o = V_p$



Thus

$$\frac{V_o}{V_p} = \frac{Z_p + Z_s}{Z_p} = 1 + \frac{Z_s}{Z_p}$$

$$B = \frac{V_p}{V_o} = \frac{Z_p}{Z_p + Z_s} = \frac{1}{1 + \frac{Z_s}{Z_p}}$$

$$B = \frac{1}{1 + \frac{Z_s}{Z_p}} = \frac{1}{1 + \frac{(1 + sRC)^2}{sRC}}$$

$$B = \frac{sRC}{(sRC)^2 + 3sRC + 1} \Rightarrow \text{Band Pass Filter}$$

Characteristic Equation

$$1 - AB = 1 - T$$

$$T = AB = \frac{\left(1 + \frac{R_2}{R_1}\right)sRC}{(sRC)^2 + 3sRC + 1}$$

$$T = \frac{1 + \frac{R_2}{R_1}}{sRC + 3 + \frac{1}{sRC}} \cdot 2$$

$$\text{If } RC = \frac{1}{\omega_o}$$

$$T(j\omega) = \frac{1 + \frac{R_2}{R_1}}{j\frac{\omega}{\omega_o} - \frac{j}{\omega/\omega_o} + 3} = \frac{1 + \frac{R_2}{R_1}}{3 + j\left(\frac{\omega}{\omega_o} - \frac{\omega_o}{\omega}\right)}$$

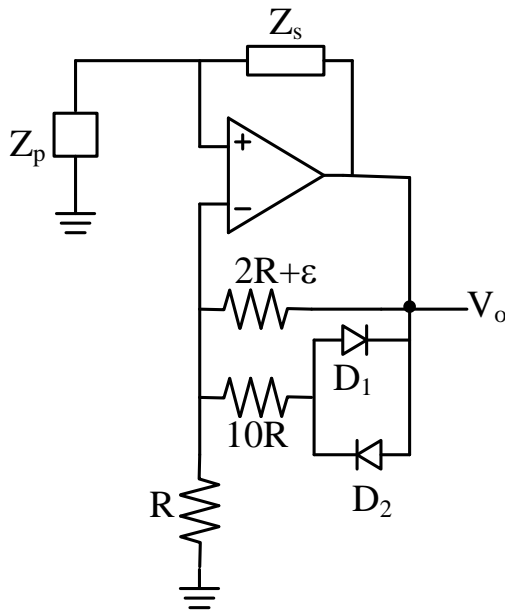
$$T(j\omega_o) = \frac{1 + R_2/R_1}{3}$$

To force oscillation

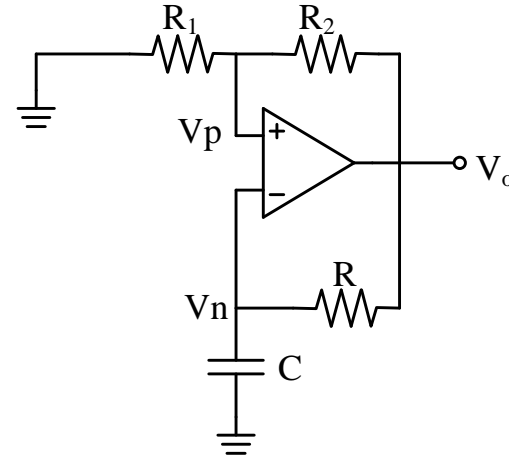
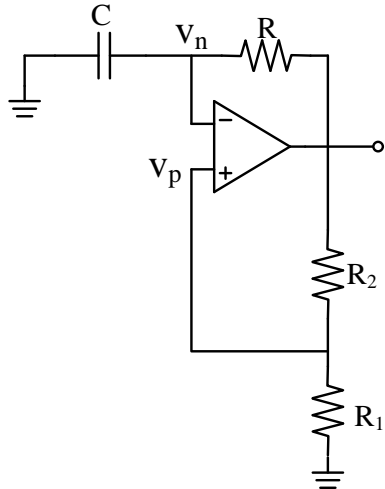
$$T(j\omega_0) > 1 \quad \text{i.e.} \quad \frac{R_2}{R_1} > 2$$

$$\frac{R_2}{R_1} = 2 + \varepsilon$$

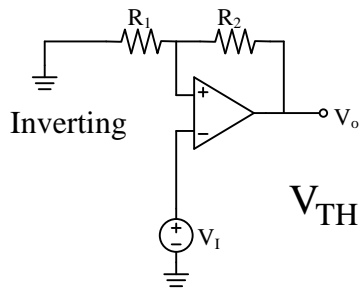
The non-linear part of the oscillator must be added if we want the comparator not to do the non-linear operation.



SQUARE WAVE OSCILLATOR



Let us look closer to the Schmitt Trigger

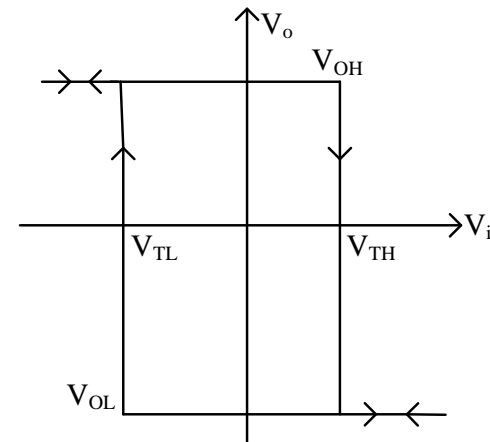


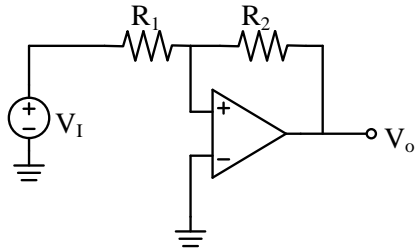
$$V_{TH} = \frac{R_1}{R_1 + R_2} V_{OH}$$

$$V_{TL} = \frac{R_1}{R_1 + R_2} V_{OL}$$

$$\Delta V_T = V_{TH} - V_{TL} = \frac{R_1}{R_1 + R_2} (V_{OH} - V_{OL})$$

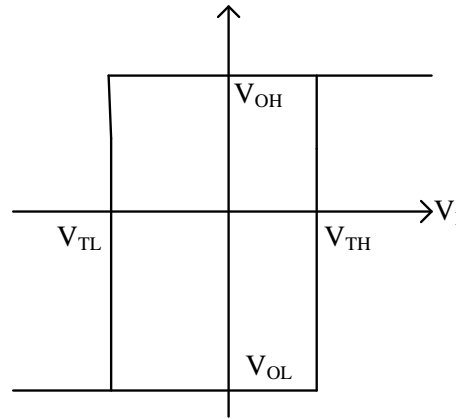
$$\Delta V_T = \frac{1}{1 + \frac{R_2}{R_1}} (V_{OH} - V_{OL})$$





Non-Inverting Schmitt Trigger

$$V_{TH} = -\frac{R_1}{R_2} V_{OL}$$



$$\frac{V_{TH} - 0}{R_1} = \frac{0 - V_{OL}}{R_2}$$

Tripping voltage V_{TL} becomes

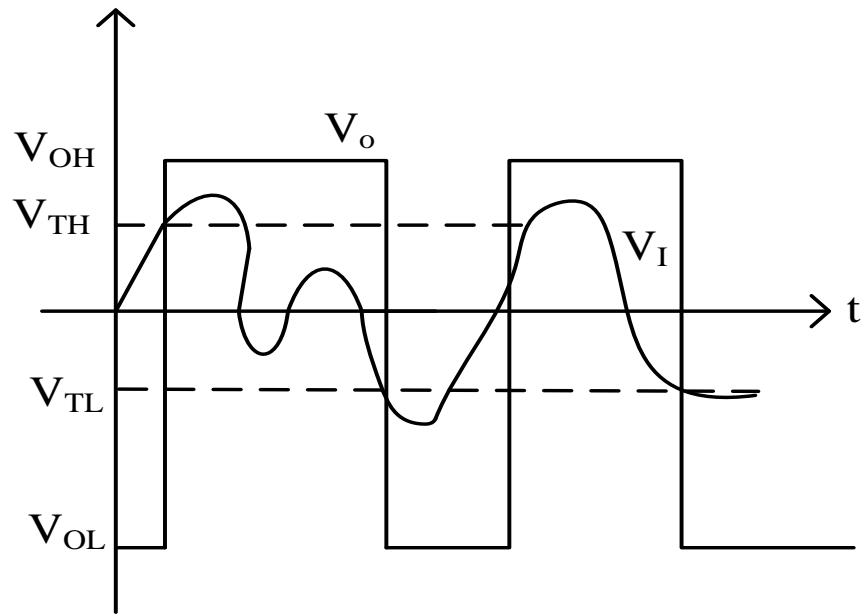
$$\frac{V_{OH} - 0}{R_2} = \frac{0 - V_{TL}}{R_1}$$

or

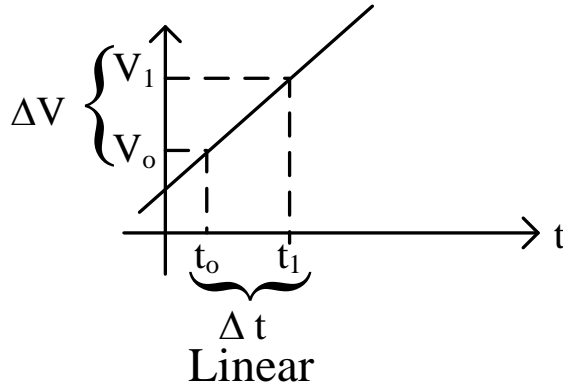
$$V_{TL} = -\frac{R_1}{R_2} V_{OH}$$

$$\Delta V_T = \frac{R_1}{R_2} (V_{OH} - V_{OL})$$

$$\Delta V_T = \frac{1}{\frac{R_2}{R_1}} (V_{OH} - V_{OL})$$

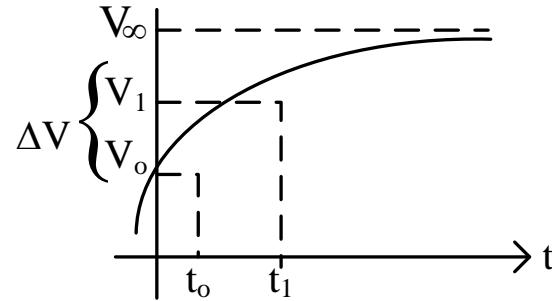


Notes on Relaxation Oscillators



$$C\Delta V = I\Delta t$$

$$\Delta t = \frac{C}{I} \Delta v$$



Exponential

$$v(t) = V_{\infty} + (V_o - V_{\infty})e^{-\frac{t-t_o}{\tau}}$$

$$\tau = RC$$

$$V_1 = V_{\infty} + (V_o - V_{\infty})e^{-\frac{t_1-t_o}{\tau}}$$

$$\Delta t = t_1 - t_o = \tau \ln \frac{V_{\infty} - V_o}{V_{\infty} - V_1}$$

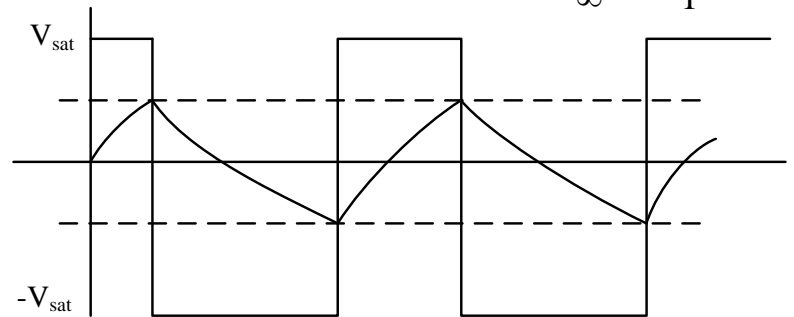
Thus for the basic-free-running exponential oscillator

$$\frac{T}{2} = RC \ln \frac{V_{sat} + V_T}{V_{sat} - V_T}$$

$$V_T = \frac{V_{sat}}{1 + \frac{R_2}{R_1}}$$

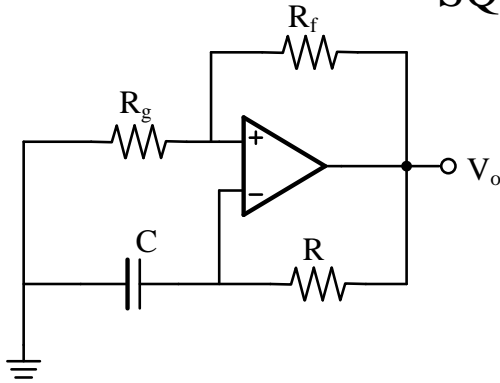
then

$$f_o = \frac{1}{T} = \frac{1}{2RC \ln(1 + 2R_1/R_2)}$$



$$f_o \neq f(V_T, V_{sat})$$

SQUARE WAVE GENERATOR



$$V_{TH} = \frac{R_g}{R_g + R_f} V_{OH}$$

or

$$V_{TL} = \frac{R_g}{R_g + R_f} V_{OL}$$

High to Low. -

Assume the output voltage is at V_{OH} , then the non-inverting input is at V_{TH} , and the inverting input is in exponential transition from its initial value V_{TL}^- toward V_{OH} . Thus

$$v^-(t) = V_{OH} - (V_{OH} - V_{TL}^-) e^{-t/RC}$$

or equivalent in the s - domain

$$V^-(s) = \frac{V_{OH}}{s} - \frac{(V_{OH} - V_{TL}^-)}{1 + s/RC}$$

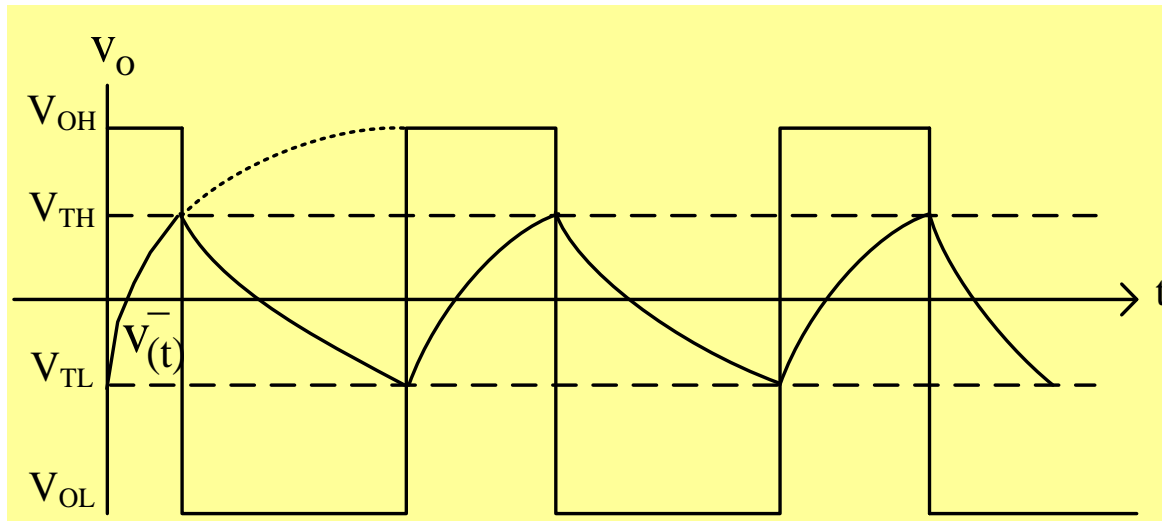
The total exponential transition time is the solution to the equality

$$v^-(t) = v_{TH}^+$$

or

$$V_{OH} - \left(V_{OH} - \frac{R_g}{R_g + R_f} V_{OL} \right) e^{-t/RC} = \frac{R_g}{R_g + R_f} V_{OH}$$

Note.- See Section 10.2 Text



Then

$$V_{OH} \left(1 - \frac{R_g}{R_g + R_f} \right) = \left(V_{OH} - \frac{R_g}{R_g + R_f} V_{OL} \right) e^{-t/RC}$$

The transition time is given by

$$t_{HL} = RC \ln \left[\frac{(R_g + R_f)V_{OH} - R_g V_{OL}}{R_f V_{OH}} \right]$$

$$t_{HL} = RC \ln \left(1 + \frac{R_g(V_{OH} - V_{OL})}{R_f V_{OH}} \right)$$

$$t_{HL} = RC \ln \left(1 + \frac{\Delta V_T}{V_{OH}} \right)$$

Low to High

Same as before by interchanging V_{OH} and V_{OL} . Then the duty cycle is determined by The sum of the transition times:

$$\tau = RC \left[\ln \left(1 + \frac{R_g (V_{OH} - V_{OL})}{R_f V_{OH}} \right) + \ln \left(1 + \frac{R_g (V_{OL} - V_{OH})}{R_f V_{OL}} \right) \right]$$
$$\tau = RC \left[\ln \left(1 + \frac{\Delta V_T}{V_{OH}} \right) + \ln \left(1 - \frac{\Delta V_T}{V_{OL}} \right) \right]$$

For 50% duty cycle $V_{OL} = -V_{OH}$ yields

$$t_{HL} = t_{LH} = RC \ln \left(1 + \frac{2R_g}{R_f} \right)$$

Then the period is given by

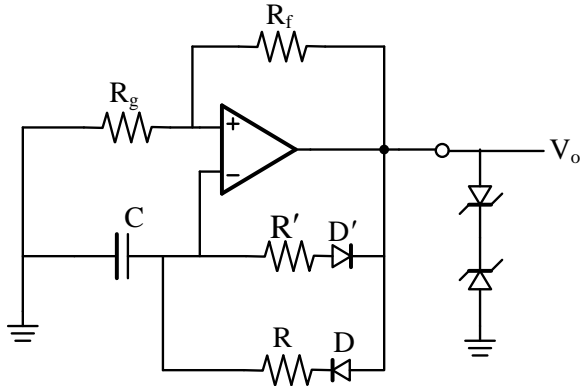
$$T = 2t_{HL} = 2RC \ln \left(1 + 2 \frac{R_g}{R_f} \right)$$

T will be affected by the SR of the comparator. Also the parasitic capacitance associated to the “+” terminal of this comparator.

Note that V_{OL} and V_{OH} cannot be exactly predicted thus often a clamping circuit is placed usually at the output.

A Stable, Nonsymmetric Square-Wave Generator

- One option is by making $-V_{OL} \neq V_{OH}$
- Another option is by changing the equality of rising and decaying times.



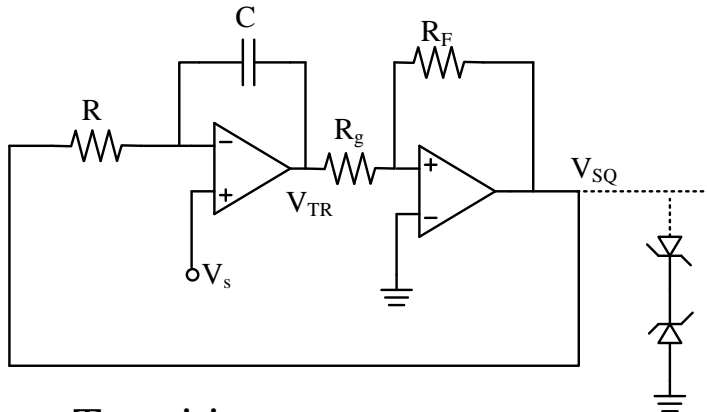
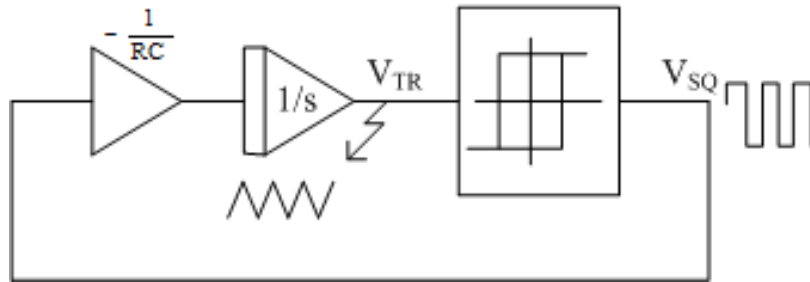
Then one can show that

$$T = t_H + t_L$$

$$T = RC \ln \left(1 + \frac{2R_g}{R_f} \right) + R'C \ln \left(1 + \frac{2R_g}{R_f} \right)$$

$$\text{Duty cycle} \triangleq \frac{t_H}{T} = \frac{R}{R + R'}$$

Basic Triangular/Square Wave Generator



- Two Quasi-static state.
- For outputs V_{OH} and V_{OL}
- The Schmitt Trigger Toggles between output states.

Transition occurs

$$V_{TR(\text{trans})} = -\frac{R_g}{R_f} V_{SQ} = \mp \frac{R_g}{R_f} V_{OH}$$

$$V_{TR} = -\frac{1}{RC} \int [V_{SQ}(t) - V_s] dt$$

When, v_{SQ} is in the high state, V_{TR} is linearly decreasing between its toggle values.

$$v_{TR} = -\frac{1}{RC} \int (V_{OH} - V_s) dt = \frac{V_s - V_{OH}}{RC} t + v_{TR}(o^+)$$

Initial condition

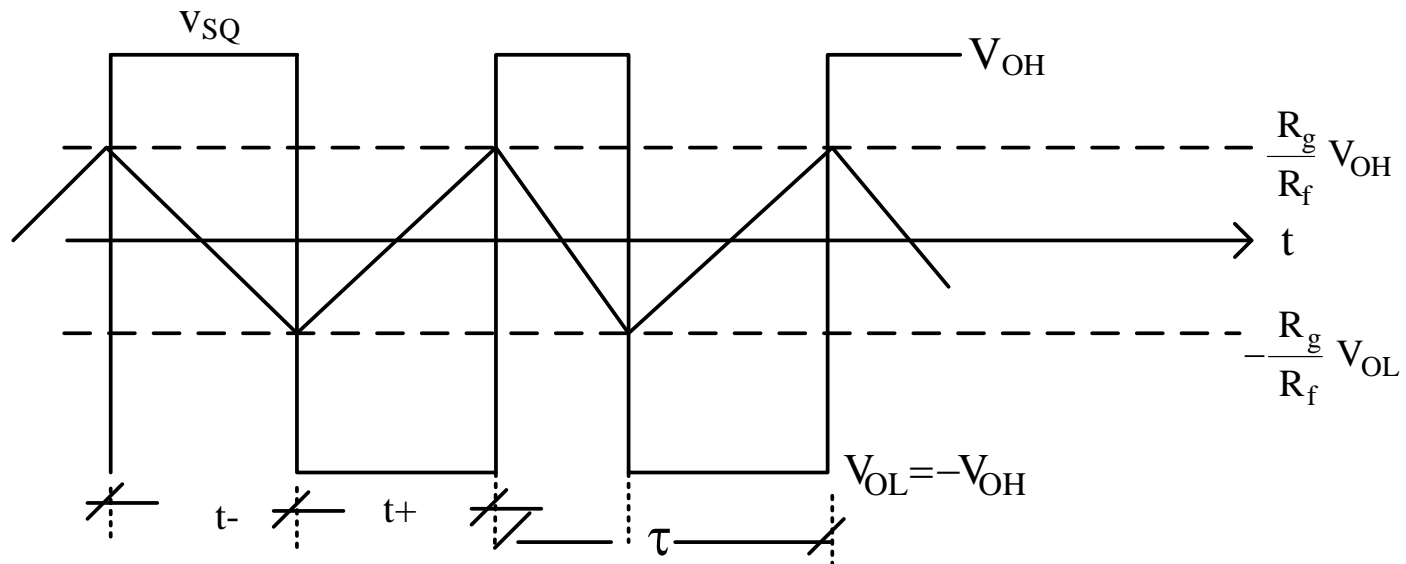
Thus, the voltage transition is the differences in toggle values divided by the slope of the linear transition.

$$2 \frac{R_g}{R_f} V_{OH} = \frac{V_{OH} - V_s}{RC} t_-$$

Therefore

$$t_- = \frac{2R_g V_{OH} \cdot RC}{R_f (V_{OH} - V_s)}$$

Now when the positive transition occurs for $V_{s>0}$



$$v_{TR} = -\frac{1}{RC} \int - (V_{OH} + V_s) dt = \frac{V_{OH} + V_s}{RC} t + v_{ti}(0^-)$$

$$2 \frac{R_g}{R_f} V_{OH} = \frac{V_{OH} + V_s}{RC} t_+ \Rightarrow t_+ = \frac{2R_g R C V_{OH}}{R_f (V_{OH} + V_s)}$$

Thus the period becomes:

$$T = t_- + t_+ = 4R_g R C \frac{V_{OH}^2}{R_f (V_{OH}^2 - V_s^2)} \Bigg|_{\text{for } V_s = 0} \cong \frac{4RC}{R_g/R_f} \quad \text{or } f_o = \frac{R_g}{4RC}$$

$$D = \text{Duty cycle} = \frac{t_+}{T} = \frac{1}{2} \left(1 - \frac{V_s}{V_{OH}} \right)$$

for $V_s = 0$, $D = 0.5$

$$\text{for } V_s = \frac{1}{4} V_{OH} \quad , \quad \text{then } D = \frac{1}{2} (1 - 0.25) = \frac{3}{8}$$